

Precision measurements of neutron beta decay II – Correlations –

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Experimentalist's approach on neutron decay

- **What can we measure?** $n \rightarrow p + e + \bar{\nu}_e$

- Neutron: spin direction σ_n
- Proton: momentum \mathbf{p}_p
- Electron: momentum \mathbf{p}_e , spin direction σ_e
- Neutrino: momentum $\mathbf{p}_\nu = -\mathbf{p}_p + \mathbf{p}_e$

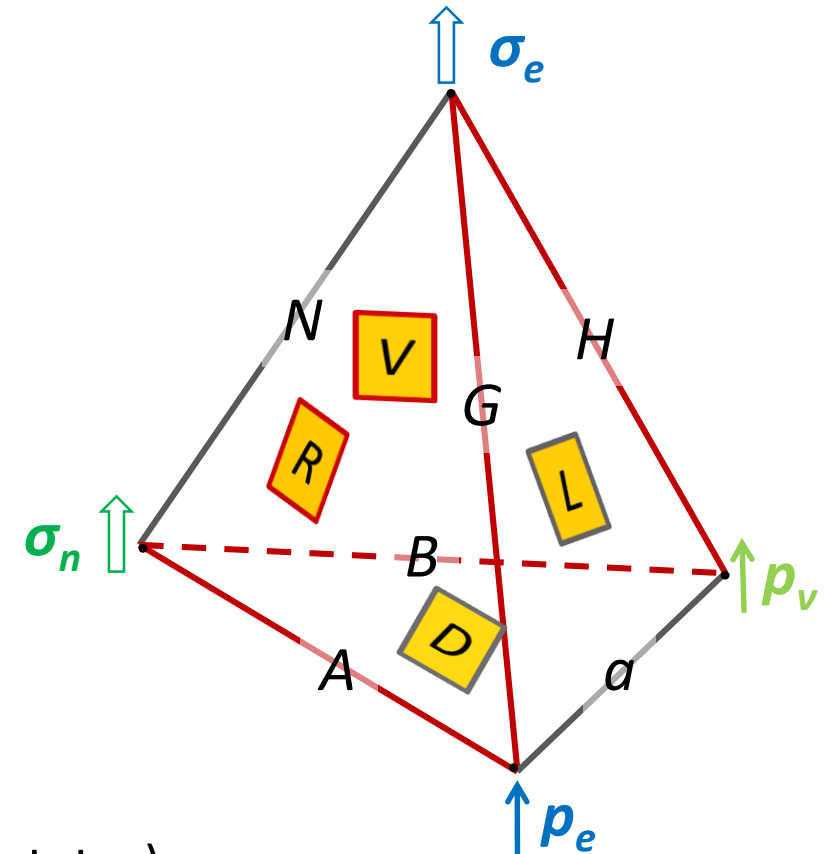
→ 2 vectors ($\mathbf{p}_e, \mathbf{p}_\nu$) & 2 axial vectors σ_n, σ_e

- **Possible correlations (this lecture):**

- 6 twofold: $\sigma_n \mathbf{p}_e, \sigma_n \mathbf{p}_\nu, \mathbf{p}_e \mathbf{p}_\nu, \dots$
- 4 threefold: $\sigma_n (\sigma_e \times \mathbf{p}_e), \dots$
- 5 fourfold: $(\sigma_e \mathbf{p}_e) (\mathbf{p}_e \mathbf{p}_\nu), \dots$
- 1 fivefold: $(\sigma_e \mathbf{p}_e) \sigma_n (\mathbf{p}_e \times \mathbf{p}_\nu)$
- + Deformation of electron spectrum (Fierz term)

- **Further observables:**

- Lifetime (lecture I)
- Rare decay modes: $n \rightarrow H + \bar{\nu}_e$ (branching ratio, H atomic states)
 $n \rightarrow p + e + \bar{\nu}_e + \gamma$ (branching ratio, even more correlations)



Content

- Principles & Concepts & Tools & Examples
 - PERKEO n : The quest for accuracy
- Status and outlook

The neutron alphabet

- $\sigma_n, \mathbf{p}_e, \mathbf{p}_\nu$: Oriented neutrons, momenta of electron and neutrino

$$dW(\langle \sigma_n \rangle | E_e, \Omega_e, \Omega_\nu) \propto G_E(E_e) \cdot \left\{ 1 + a \frac{\mathbf{p}_e \mathbf{p}_\nu}{E_e E_\nu} + b \frac{m_e}{E_e} + \frac{\langle \sigma_n \rangle}{\sigma_n} \left(A \frac{\mathbf{p}_e}{E_e} + B \frac{\mathbf{p}_\nu}{E_\nu} + D \frac{\mathbf{p}_e \times \mathbf{p}_\nu}{E_e E_\nu} \right) \right\}$$

- $\sigma_e, \mathbf{p}_e, \mathbf{p}_\nu$: Spin and momentum of electron, momentum of neutrino

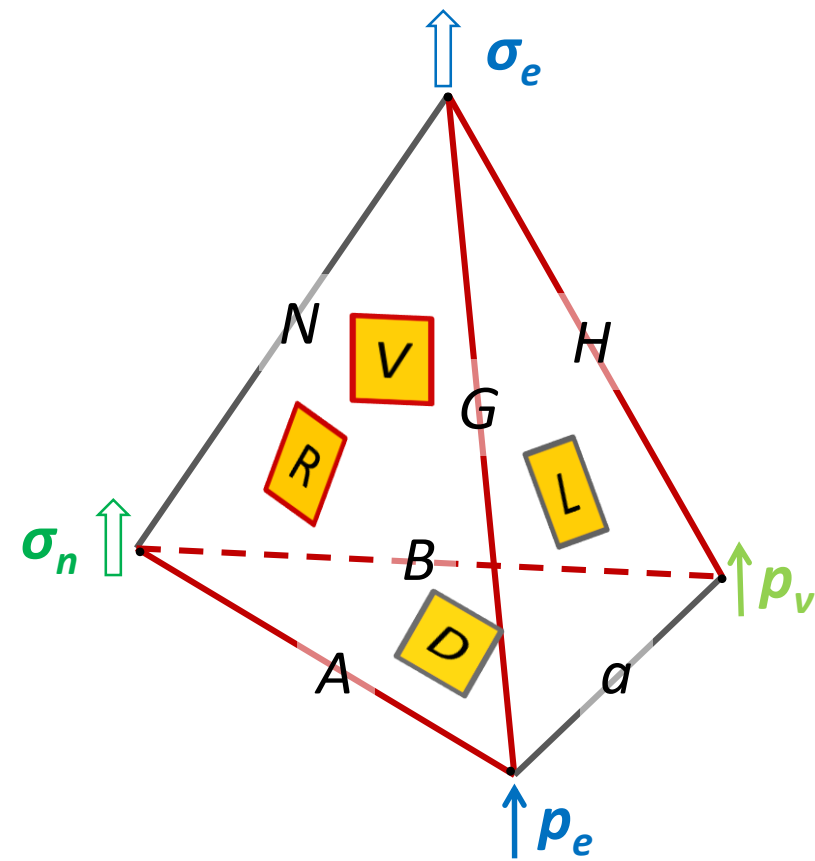
$$dW(\langle \sigma_e \rangle | E_e, \Omega_e, \Omega_\nu) \propto G_E(E_e) \cdot \left\{ 1 + a \frac{\mathbf{p}_e \mathbf{p}_\nu}{E_e E_\nu} + b \frac{m_e}{E_e} + \frac{\langle \sigma_e \rangle}{\sigma_e} \left(G \frac{\mathbf{p}_e}{E_e} + H \frac{\mathbf{p}_\nu}{E_\nu} + K \frac{\mathbf{p}_e}{E_e + m_e} \frac{\mathbf{p}_e \mathbf{p}_\nu}{E_e E_\nu} + L \frac{\mathbf{p}_e \times \mathbf{p}_\nu}{E_e E_\nu} \right) \right\}$$

- $\sigma_n, \sigma_e, \mathbf{p}_e$: Oriented neutrons, momentum and spin of electron

$$dW(\langle \sigma_n \rangle, \langle \sigma_e \rangle | E_e, \Omega_e) \propto G_E(E_e) \cdot \left\{ 1 + b \frac{m_e}{E_e} + \frac{\langle \sigma_n \rangle}{\sigma_n} A \frac{\mathbf{p}_e}{E_e} + \frac{\langle \sigma_e \rangle}{\sigma_e} \left(G \frac{\mathbf{p}_e}{E_e} + N \frac{\langle \sigma_n \rangle}{\sigma_n} + Q \frac{\mathbf{p}_e}{E_e + m_e} \frac{\langle \sigma_n \rangle \mathbf{p}_e}{\sigma_n E_e} + R \frac{\langle \sigma_n \rangle \times \mathbf{p}_e}{\sigma_n E_e} \right) \right\}$$

- $\sigma_n, \sigma_e, \mathbf{p}_e, \mathbf{p}_\nu$: Oriented neutrons, spin and momentum of electron, momentum of and neutrino

$$dW(\langle \sigma_n \rangle, \langle \sigma_e \rangle | E_e, \Omega_e, \Omega_\nu) \propto G_E(E_e) \cdot \left\{ 1 + \begin{array}{l} \text{All terms} \\ \text{from above} \end{array} + \frac{\langle \sigma_n \rangle}{\sigma_n} \left(S \frac{\langle \sigma_e \rangle \mathbf{p}_e \mathbf{p}_\nu}{\sigma_e E_e E_\nu} + T \frac{\mathbf{p}_\nu \langle \sigma_e \rangle \mathbf{p}_e}{E_\nu \sigma_e E_e} + U \frac{\mathbf{p}_e \langle \sigma_e \rangle \mathbf{p}_\nu}{E_e \sigma_e E_\nu} + V \frac{\langle \sigma_e \rangle \times \mathbf{p}_\nu}{\sigma_e E_\nu} + W \frac{\langle \sigma_e \rangle \mathbf{p}_e}{\sigma_e (E_e + m_e)} \frac{\mathbf{p}_e \times \mathbf{p}_\nu}{E_e E_\nu} \right) \right\}$$



Challenges in $n \rightarrow pev$, $m_n - m_p - m_e = 782 \text{ keV}$

Proton energy $E_p < 751 \text{ eV}$

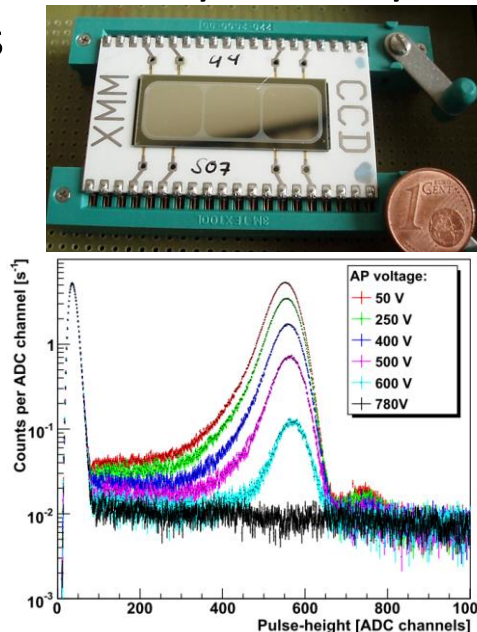
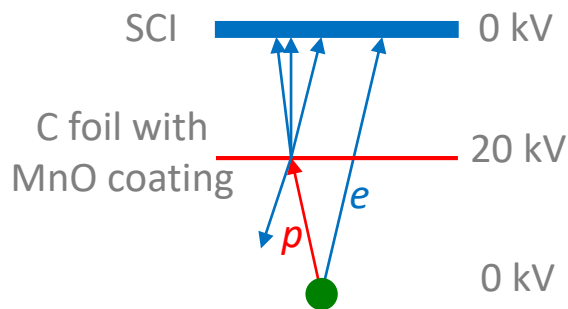
→ Sensitive to small electric fields

- ✓ Control space charges
- ✓ Control work functions of surfaces
- ✓ Control field leakages

→ Acceleration needed prior to detection

→ Optimized detectors

- ✓ Low noise, low thresholds, tiny dead layers
- ✓ Specific technologies



Electron energy $E_e < 782 \text{ keV}$

→ Range of background from (n, γ) , beta decays

- ✓ Shielding
- ✓ Magnetic fields for Signal/Background
- ✓ Coincidences (ΔE - E detectors, proton)

→ Exposed to backscattering by detector and scattering by windows/materials

- ✓ Backscatter-suppression or detection
- ✓ Proper design of spectrometer

Long lifetime $\tau_n \approx 880 \text{ s}$

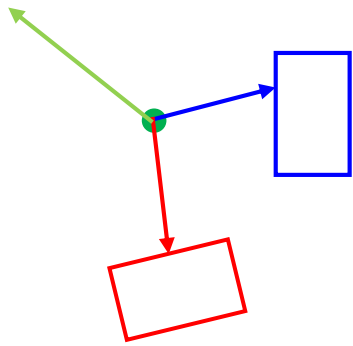
→ Low decay rate, low statistics

→ Low relative decay rate for cold neutrons
 $\sim 1000 \text{ m/s}: \sim 10^{-7} / \text{m}$

→ All other neutrons can create background

- Captures (n, γ) , ...
- Scattering from apertures $\sim 10^{-3}$

Detector geometry – principles



$\mathbf{K}_{i,\parallel}$: \parallel to detectors' surfaces, \perp to plane of drawing

$\mathbf{K}_{i,\perp}$: \perp to $\mathbf{K}_{i,\parallel}$, i.e. in plane of drawing (not necessarily \perp on detector surface)

K	e	p	ep
b	K	K	K
a	0	0	K
A, \perp	K	K	K
A, \parallel	0	0	0
B, \perp	0	K	K
B, \parallel	0	0	0
D, \perp	0	0	0
D, \parallel	0	0	K

$$dW(\langle \sigma_n \rangle | E_e, \Omega_e, \Omega_v) \propto G_E(E_e) \cdot \left\{ 1 + a \frac{\mathbf{p}_e \mathbf{p}_v}{E_e E_v} + b \frac{m_e}{E_e} + \mathbf{P} \left(A \frac{\mathbf{p}_e}{E_e} + B \frac{\mathbf{p}_v}{E_v} + D \frac{\mathbf{p}_e \times \mathbf{p}_v}{E_e E_v} \right) \right\}$$

$$K_a = \int_{e\text{Det}, p\text{Det}} G_E(E_e) \frac{\mathbf{p}_e \mathbf{p}_v}{E_e E_v} dE_e d\Omega_e d\Omega_v$$

$$K_A = \int_{e\text{Det}, p\text{Det}} G_E(E_e) \frac{\mathbf{p}_e}{E_e} dE_e d\Omega_e d\Omega_v$$

$$K_b = \int_{e\text{Det}, p\text{Det}} G_E(E_e) \frac{m_e}{E_e} dE_e d\Omega_e d\Omega_v$$

$$K_B = \int_{e\text{Det}, p\text{Det}} G_E(E_e) \frac{\mathbf{p}_v}{E_v} dE_e d\Omega_e d\Omega_v$$

Often analysis in function of E_e (i.e. $K_i = K_i(E_e)$, no integration over E_e)

$$K_D = \int_{e\text{Det}, p\text{Det}} G_E(E_e) \frac{\mathbf{p}_e \times \mathbf{p}_v}{E_e E_v} dE_e d\Omega_e d\Omega_v$$

$$N_{e,p} \propto 1 + aK_a + bK_b + \mathbf{P}(AK_A + BK_B + DK_D)$$

Asymmetries with neutron spin:

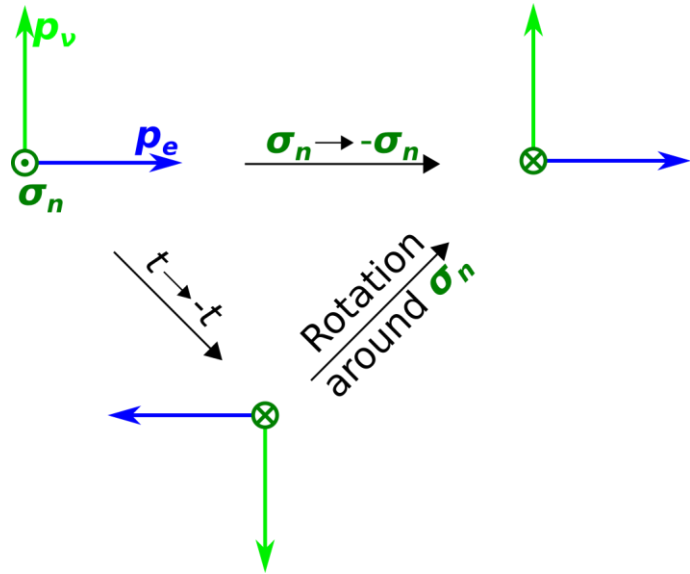
$$\alpha = \frac{N_{e,p}(\mathbf{P}) - N_{e,p}(-\mathbf{P})}{N_{e,p}(\mathbf{P}) + N_{e,p}(-\mathbf{P})} = \frac{\mathbf{P}(AK_A + BK_B + DK_D)}{1 + aK_a + bK_b}$$

Goals of detector design:

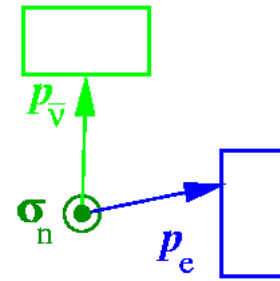
- Maximize sensitivity to wanted coefficient i
 - Maximize K_i
 - Maximize statistics
- Suppress other coefficients
 - Suppress by symmetry or minimize $K_{j \neq i}$

Example D : Discrete symmetries and detector design

$$dW \propto 1 + D \frac{\langle \sigma_n \rangle}{\sigma_n} \frac{\mathbf{p}_e \times \mathbf{p}_v}{E_e E_v}$$

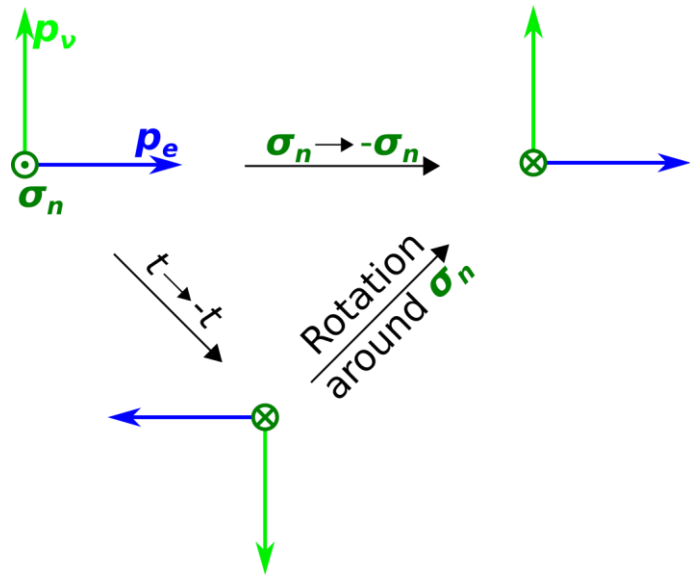


Principle Set-Up

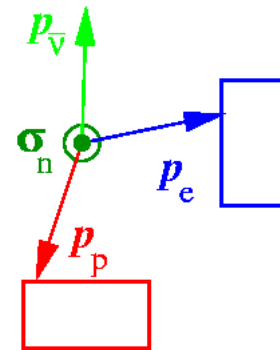


Example D : Discrete symmetries and detector design

$$dW \propto 1 + D \frac{\langle \sigma_n \rangle}{\sigma_n} \frac{\mathbf{p}_e \times \mathbf{p}_v}{E_e E_v}$$



Principle Set-Up



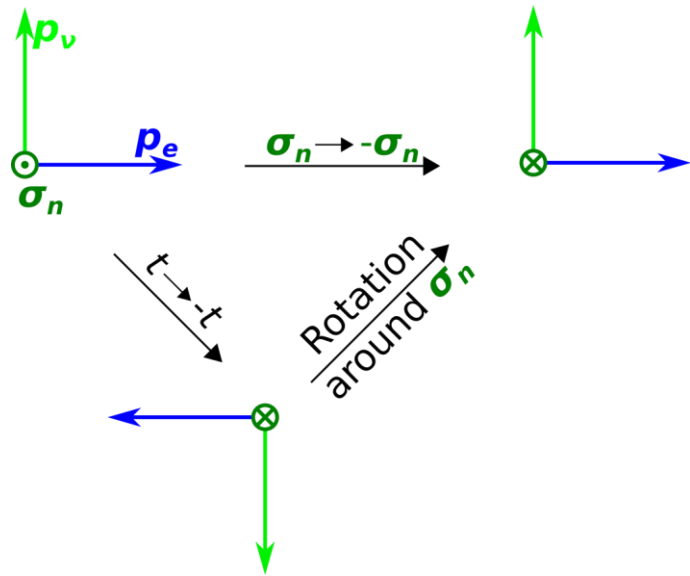
$$\kappa_\xi = \frac{K_\xi}{1 + aK_a + bK_b}$$

$$\alpha = \frac{n_{ep}^{\odot} - n_{ep}^{\otimes}}{n_{ep}^{\odot} + n_{ep}^{\otimes}} = DP\kappa_D$$

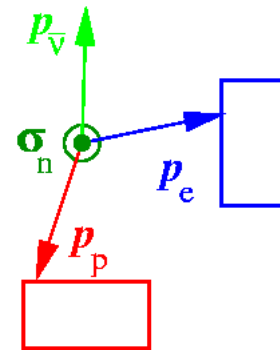
Example D : Discrete symmetries and detector design

$$dW(\langle \sigma_n \rangle | E_e, \Omega_e, \Omega_v) \propto G_E(E_e) \cdot \left\{ 1 + a \frac{\mathbf{p}_e \mathbf{p}_v}{E_e E_v} + b \frac{m_e}{E_e} + \frac{\langle \sigma_n \rangle}{\sigma_n} \left(A \frac{\mathbf{p}_e}{E_e} + B \frac{\mathbf{p}_v}{E_v} \right) + D \frac{\langle \sigma_n \rangle \mathbf{p}_e \times \mathbf{p}_v}{\sigma_n E_e E_v} \right\}$$

P violating, asymmetry
with spin flip



Principle Set-Up



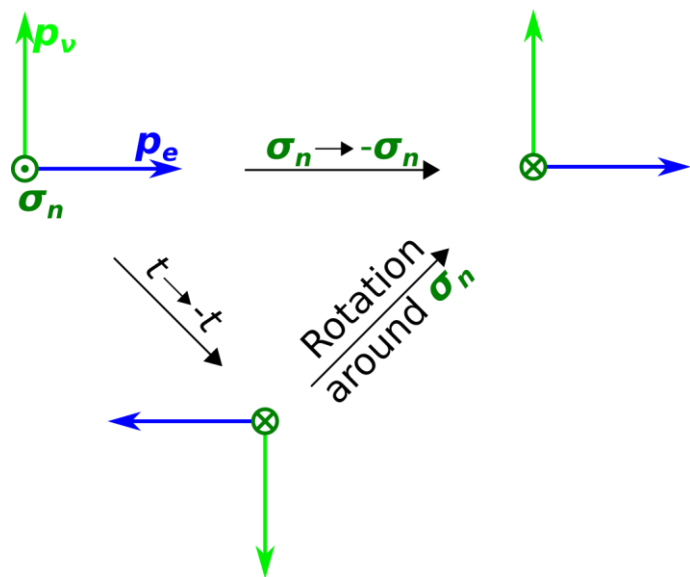
$$\kappa_\xi = \frac{K_\xi}{1 + aK_a + bK_b}$$

$$\alpha = \frac{n_{ep}^\odot - n_{ep}^\otimes}{n_{ep}^\odot + n_{ep}^\otimes} = DP\kappa_D + AP\kappa_A + BP\kappa_B$$

Example *D*: Discrete symmetries and detector design

$$dW(\langle \sigma_n \rangle | E_e, \Omega_e, \Omega_\nu) \propto G_E(E_e) \cdot \left\{ 1 + a \frac{\mathbf{p}_e \mathbf{p}_\nu}{E_e E_\nu} + b \frac{m_e}{E_e} + \frac{\langle \sigma_n \rangle}{\sigma_n} \left(A \frac{\mathbf{p}_e}{E_e} + B \frac{\mathbf{p}_\nu}{E_\nu} \right) + D \frac{\langle \sigma_n \rangle \mathbf{p}_e \times \mathbf{p}_\nu}{\sigma_n E_e E_\nu} \right\}$$

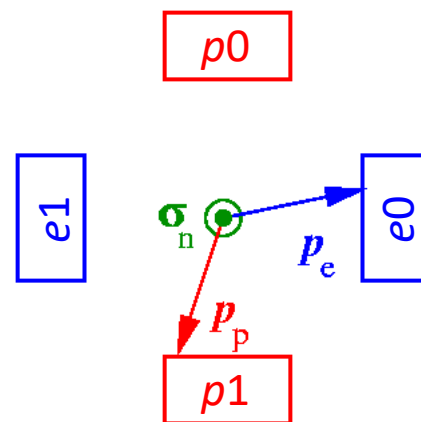
P violating, asymmetry
with spin flip



Suppression of parity-violating correlations if detector setup and neutron volume share two orthogonal mirror planes

Breaking of symmetry → Systematic effects

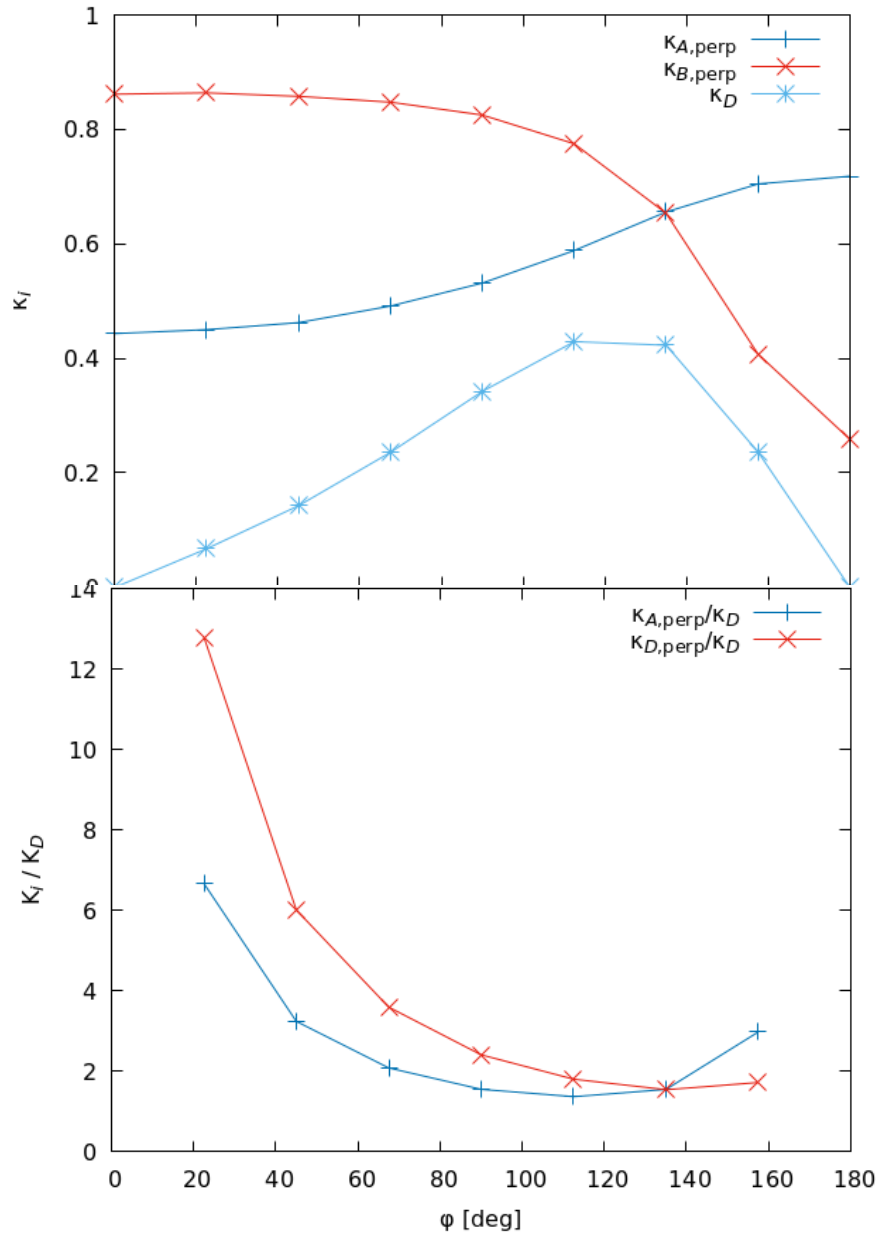
Principle Set-Up



$$D = \frac{\alpha^{00} - \alpha^{01} - \alpha^{10} + \alpha^{11}}{4P\kappa_D^{00}}$$

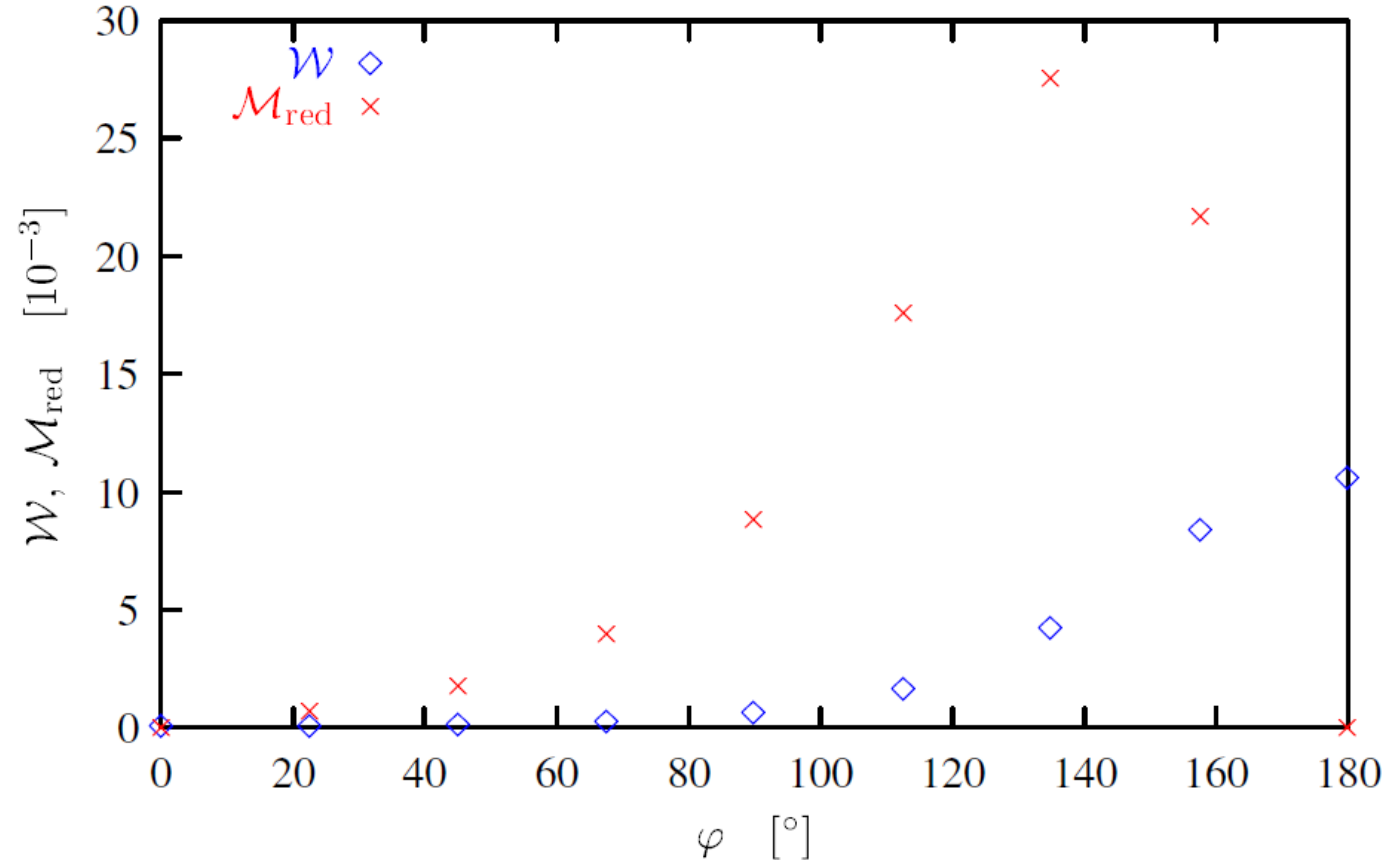
$$\kappa_\xi = \frac{K_\xi}{1 + aK_a + bK_b}$$

D: Detector design – Minimizing and maximizing



← **Minimize** $\kappa_{A,B}/\kappa_D$

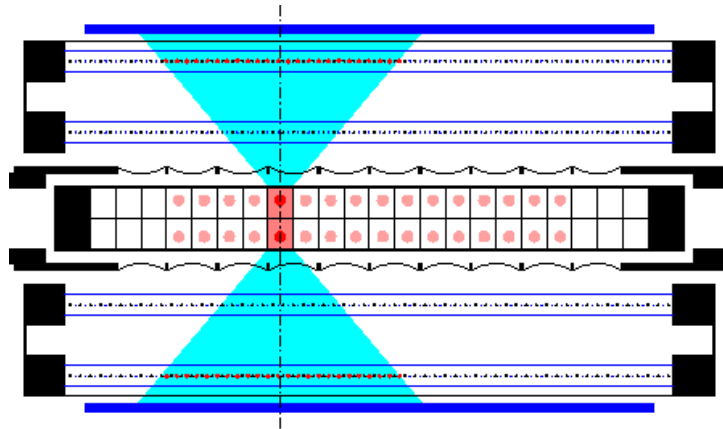
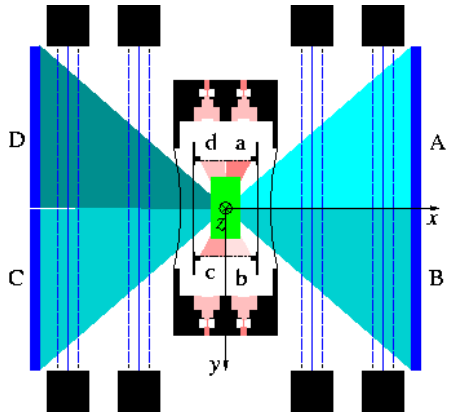
↓ **Maximize** Figure of merit $w(P\kappa_D)^2$



D: Status

Trine

- Electron tracking



Leading systematics:

- Inhomogeneity of MWPC
- Asymmetry of beam profile
- Asymmetry of scintillator

TS et al, Phys. Lett. B 581 (2004) 49

$$D = (-2.8 \pm 6.4^{\text{stat}} \pm 3.0^{\text{syst}}) \cdot 10^{-4}$$

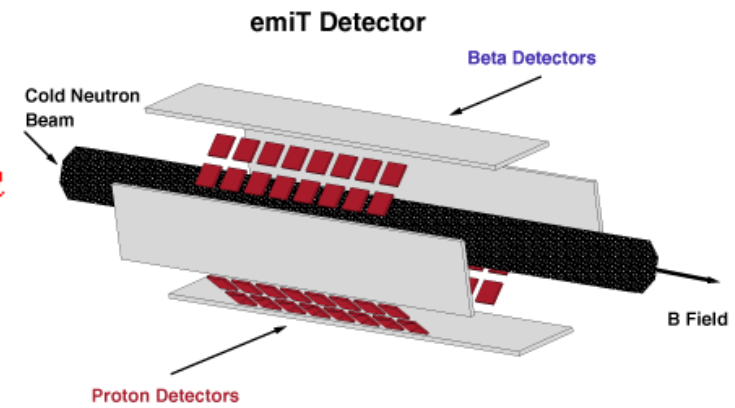
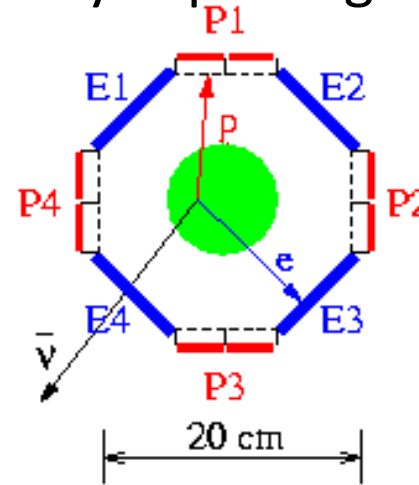
Measurements of “0” systematically easier than absolute measurements:

- One “just” needs a symmetric detector
- Most systematic effects scale with the measured asymmetry

Theory says: EDMs are more sensitive than $\overline{\text{TR}}$ searches in n decay ... ☹

emiT

- Fully exploits geometrical optimization

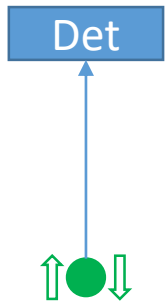


Chupp et al, Phys.Rev. C 86 (2012) 035505

$$D = (-0.94 \pm 1.89^{\text{stat}} \pm 0.97^{\text{syst}}) \cdot 10^{-4}$$

How to measure spin asymmetries

$$dW(\mathbf{P}_n | E_e, \Omega_e) \propto G_E(E_e) \cdot \left(1 + A \frac{P_n p_e}{E_e}\right) \quad (\text{observe only electron} \rightarrow \Omega_\nu \text{ integrated out. } \frac{\langle \sigma_n \rangle}{\sigma_n} \equiv P_n)$$



$$N_{\uparrow\downarrow}(E_e) = \text{const} \cdot G_E(E_e) \cdot \int_{\text{Det}} \{1 \pm A P_n \beta(E_e) \cos(\angle(\mathbf{P}_n, \mathbf{p}_e))\} d\Omega_e \quad \frac{p_e}{E_e} = \beta(E_e) \equiv \frac{v_e}{c}$$

$$k = k(\text{Det, Beam}) = \left\langle \int_{\text{Det}} \cos(\angle(\mathbf{P}_n, \mathbf{p}_e)) d\Omega_e \right\rangle_{\text{Beam}}$$

$$\frac{N_{\uparrow\uparrow} - N_{\downarrow\uparrow}}{N_{\uparrow\uparrow} + N_{\downarrow\uparrow}}(E_e) = A \beta(E_e) k P_n$$

We need:

- Polarization P_n
- **Identical polarization** (and amount of neutrons) in both states
- Precise detector solid angle with respect to polarized neutrons k
- Electron energy $\beta = \beta(E_e)$

Sensitive to neutron flux variations in first order!

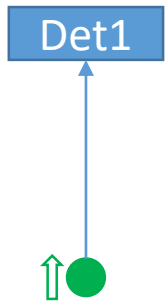
If flipping efficiency (probability that a spin gets flipped) $f < 1$:

- Polarization after flipper: $P_\downarrow = -(2f - 1)P_\uparrow$
- Resulting asymmetry:

$$\frac{N_{\uparrow\uparrow} - N_{\downarrow\uparrow}}{N_{\uparrow\uparrow} + N_{\downarrow\uparrow}} = A \beta k P_n f \cdot [1 - A \beta k P_n (1 - f) + \mathcal{O}((A \beta k P_n (1 - f))^2)]$$

How to measure spin asymmetries

$$dW(\mathbf{P}_n | E_e, \Omega_e) \propto G_E(E_e) \cdot \left(1 + A \frac{\mathbf{P}_n \mathbf{p}_e}{E_e} \right) \quad (\text{observe only electron} \rightarrow \Omega_\nu \text{ integrated out. } \frac{\langle \sigma_n \rangle}{\sigma_n} \equiv \mathbf{P}_n)$$



$$N_{\uparrow 2}^1(E_e) = \text{const} \cdot G_E(E_e) \cdot \int_{\text{Det}_2^1} \{1 + A P_n \beta(E_e) \cos(\angle(\mathbf{P}_n, \mathbf{p}_e))\} d\Omega_e \quad \frac{p_e}{E_e} = \beta(E_e) \equiv \frac{v_e}{c}$$

$$k_i = k(\text{Det } i, \text{Beam}) = \left\langle \int_{\text{Det } i} \cos(\angle(\mathbf{P}_n, \mathbf{p}_e)) d\Omega_e \right\rangle_{\text{Beam}}$$

$$\frac{N_{\uparrow\uparrow} - N_{\uparrow\downarrow}}{N_{\uparrow\uparrow} + N_{\uparrow\downarrow}}(E_e) = A \beta(E_e) k P_n$$



Insensitive to neutron flux variations!

But to Det1 ≠ Det2

We need:

- Polarization P_n
- 2 **identical detectors** (same efficiency, same response)
- Precise detector solid angle with respect to polarized neutrons k
- Electron energy $\beta = \beta(E_e)$

With different detectors k_i : $\bar{k} \equiv \frac{k_1 + k_2}{2}$, $\Delta_{k,rel} \equiv \frac{k_1 - k_2}{k_1 + k_2}$

- Resulting asymmetry:

$$\frac{N_{\uparrow\uparrow} - N_{\uparrow\downarrow}}{N_{\uparrow\uparrow} + N_{\uparrow\downarrow}} = A \beta \bar{k} P_n \cdot \left[1 - A \beta \bar{k} P_n \Delta_{k,rel} + \mathcal{O}\left((A \beta \bar{k} P_n \Delta_{k,rel})^2\right) \right]$$

How to measure spin asymmetries

Two detectors + neutron spin flipping

Det1

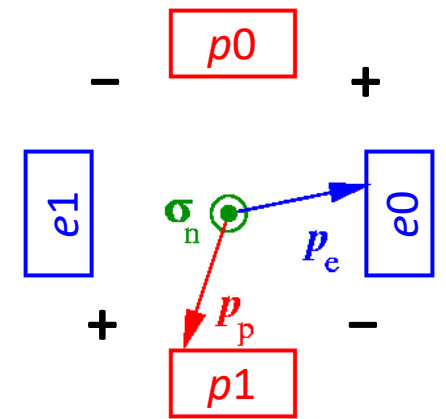


$$A_{\text{exp},1} \equiv \frac{N_{\uparrow\uparrow} - N_{\downarrow\uparrow}}{N_{\uparrow\uparrow} + N_{\downarrow\uparrow}} = A\beta k_1 P_n f$$

Det2

$$A_{\text{exp},2} \equiv \frac{N_{\uparrow\downarrow} - N_{\downarrow\downarrow}}{N_{\uparrow\downarrow} + N_{\downarrow\downarrow}} = -A\beta k_2 P_n f$$

Note: for D this applies, too:



→ Measures both signs of the asymmetry at the same time

- **Analysis by detector, arithmetic average of both results** $A = \frac{A_1 + A_2}{2}$ or **joint fit**

→ Suppresses neutron flux fluctuations in first order
 → Compensates some systematics (e.g. shift of beam towards one detector), depending on experiment

- **Super-ratio of detector rates:**

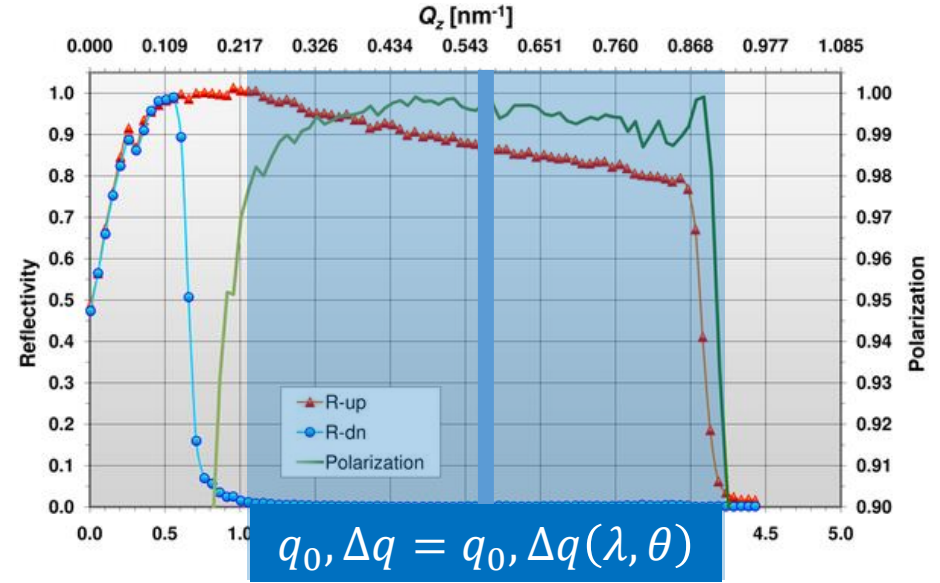
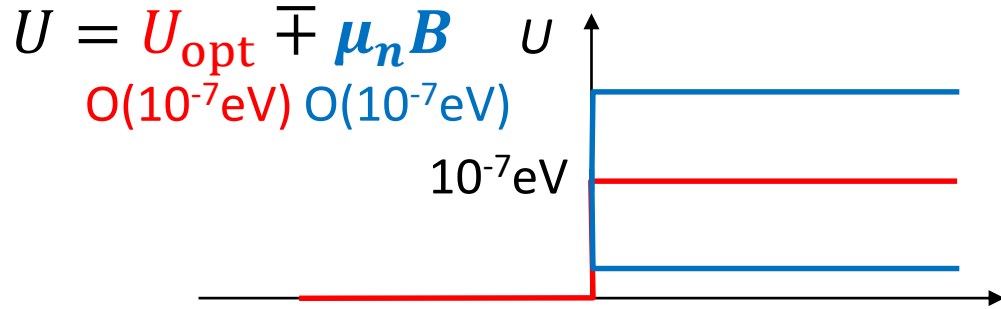
$$A_{\text{SR}} = \frac{1 - \sqrt{R}}{1 + \sqrt{R}} = A\beta k P_n, \text{ with } R = \frac{N_{\uparrow\uparrow} N_{\downarrow\downarrow}}{N_{\downarrow\uparrow} N_{\uparrow\downarrow}}$$

→ Neutron flux fluctuations fully cancel

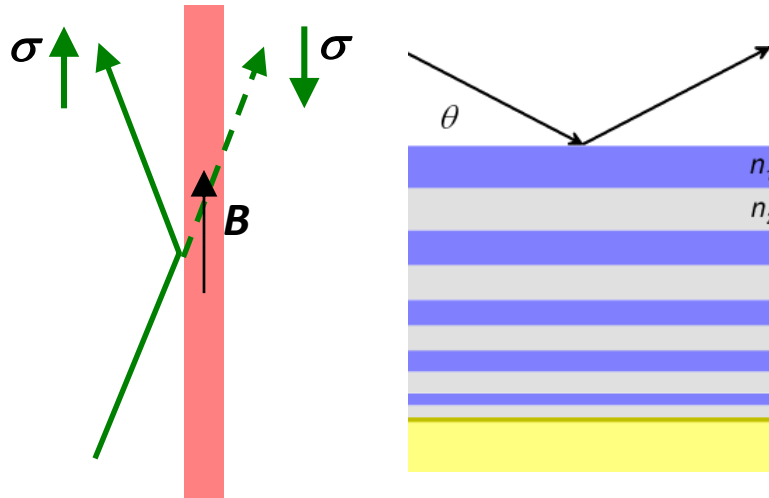
- Both have similar sensitivity to Δ_k and to $f < 1$

Cold neutron polarization in a nutshell

Magnetic mirrors and supermirrors



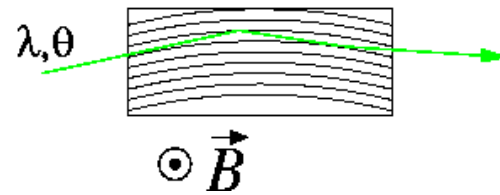
Match index of refraction



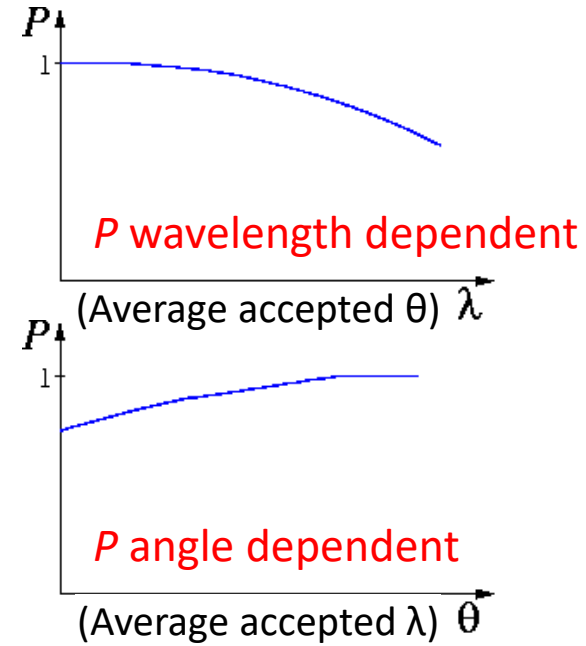
Increase critical angle

Polarizing benders

➤ No passage without reflection

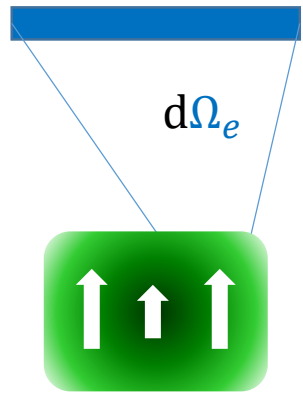


➤ Typical performance:
 $\langle P \rangle_{\text{Beam}} \sim 98\%$



Neutron polarization and systematics

Beam average may not be relevant!



$$dW \propto 1 + A \frac{P_n p_e}{E_e}$$

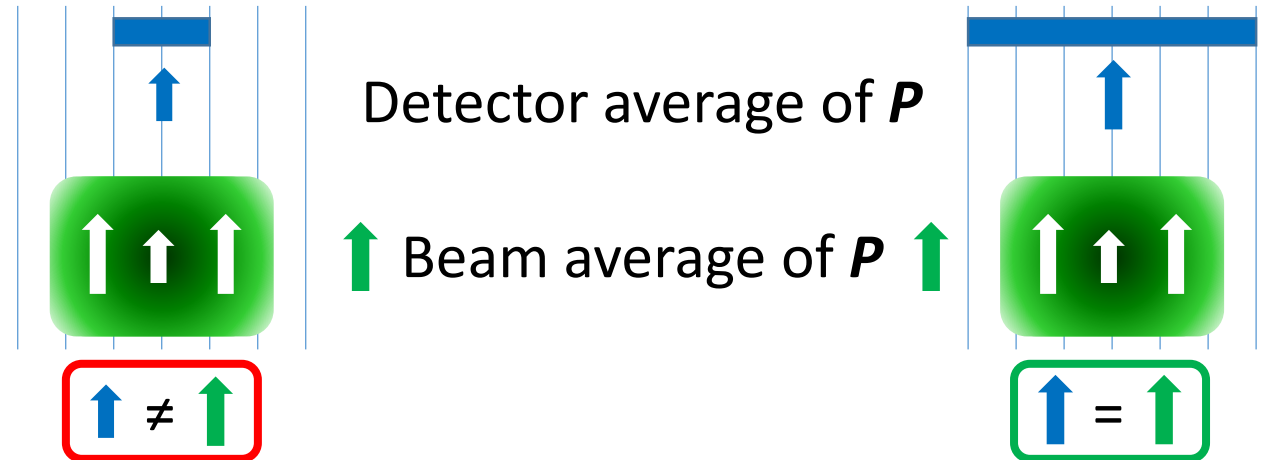
$$\frac{N_{\uparrow} - N_{\downarrow}}{N_{\uparrow} + N_{\downarrow}} \propto A \left\langle \int_{\text{Det}} P_n p_e d\Omega_e \right\rangle_{\text{Beam}}$$

$$\left\langle \int_{\text{Det}} P_n p_e d\Omega_e \right\rangle_{\text{Beam}} \neq \langle P_n \rangle_{\text{Beam}} \left\langle \int_{\text{Det}} p_e d\Omega_e \right\rangle_{\text{Beam}}$$

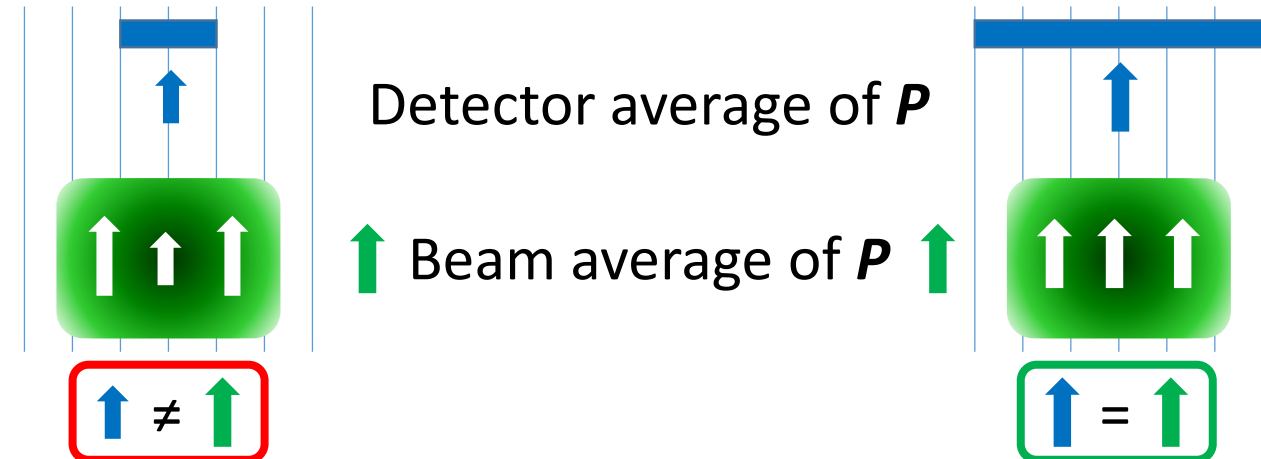
Neutron beams are large, divergent, inhomogeneous

Solutions

1) *Detector averages beam (requires mag field)*

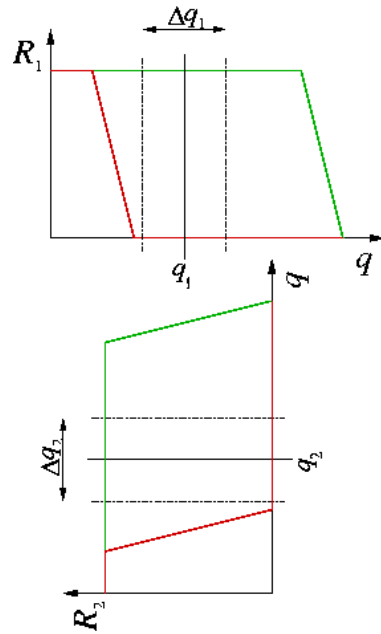
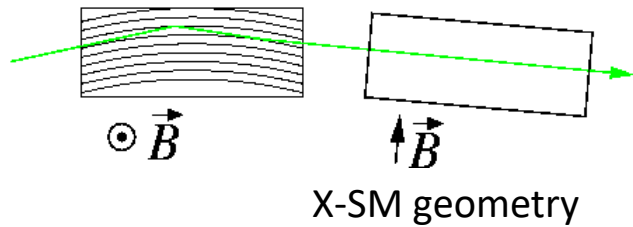
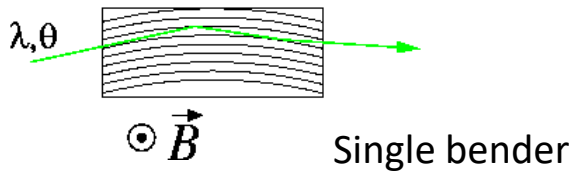


2) *"Perfect" polarization (here: homogeneous)*



(Almost) perfect polarization

X-SM geometry

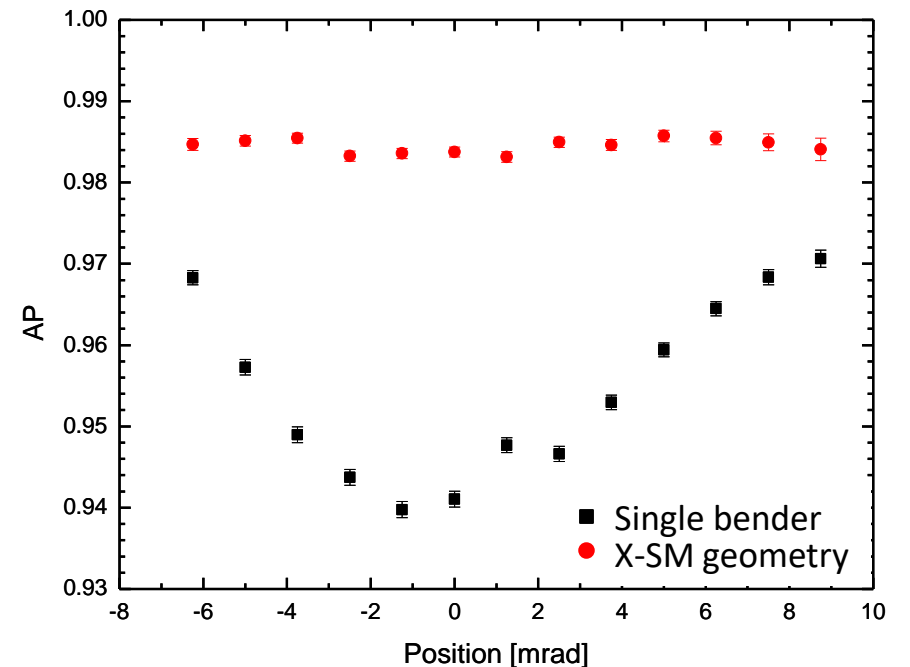
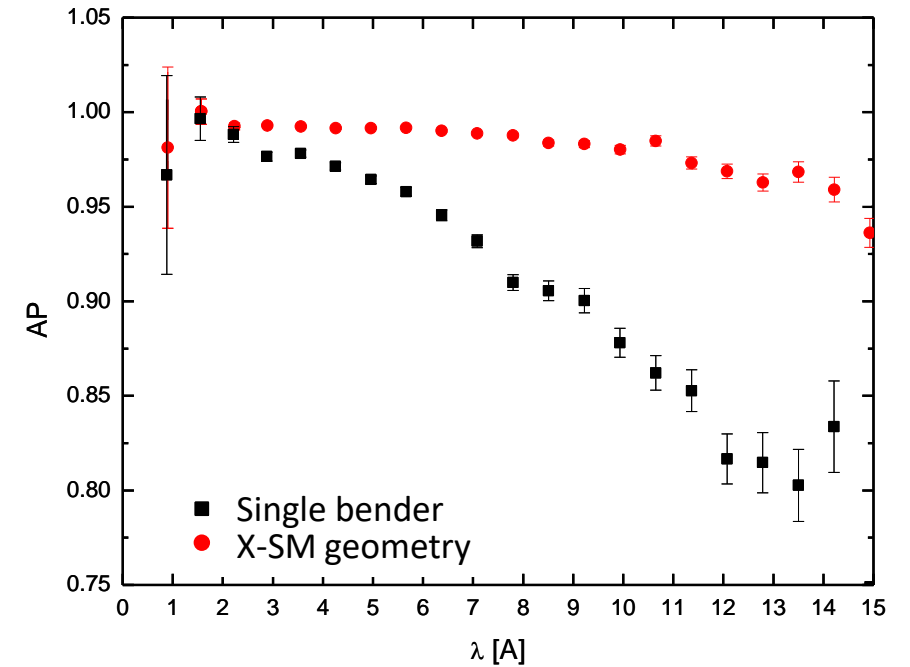


$$P_x = \frac{P_1 + P_2}{1 + P_1 P_2} \approx 1 - \frac{1}{2} (1 - P)^2$$

→ Imperfections suppressed quadratically

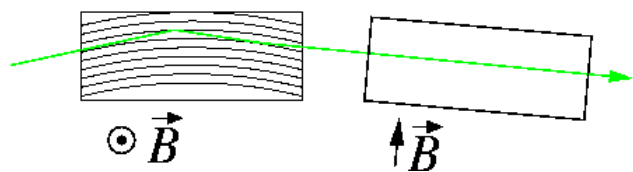
→ Dependences on λ , θ strongly reduced

$$T_{1 \times 2} = T_1 T_2$$



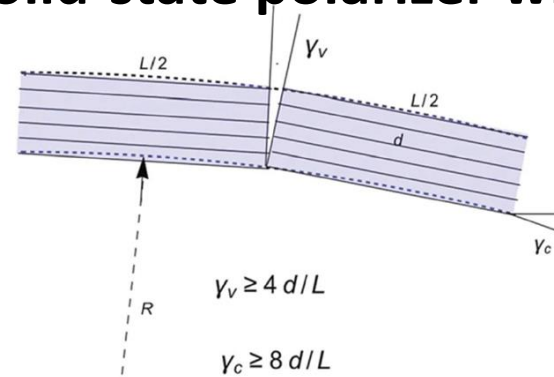
(Almost) perfect polarization

X-SM geometry

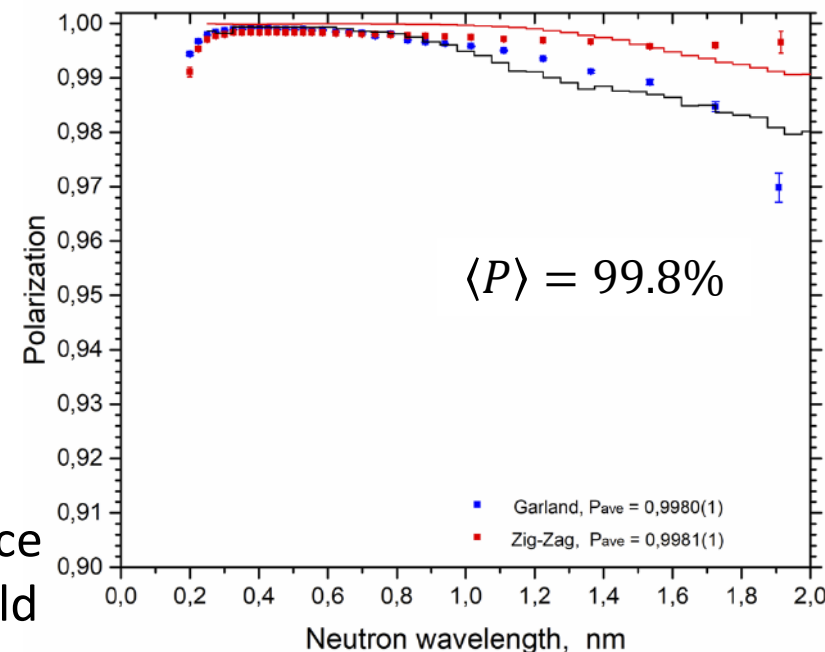


$$P_x \approx 1 - \frac{1}{2}(1 - P)^2, \quad T_{1 \times 2} = T_1 T_2$$

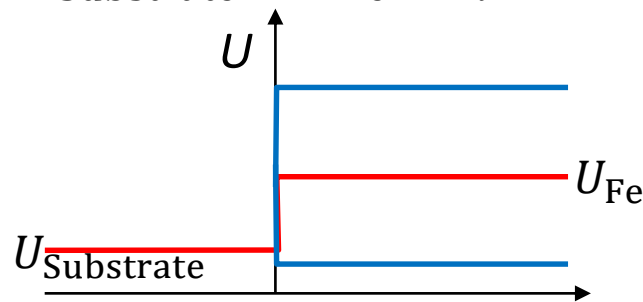
Solid-state polarizer with quartz or sapphire substrate



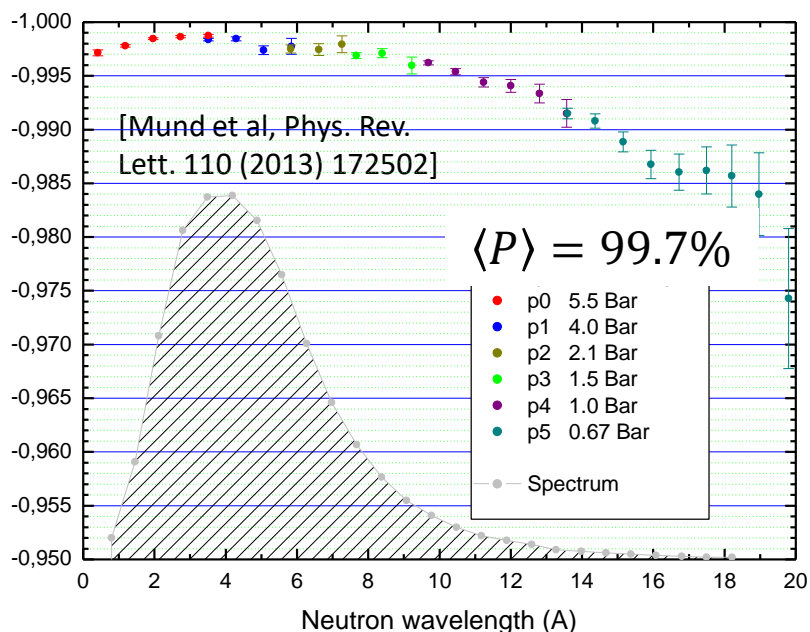
Garland vs Zig-Zag



- Finite minimum angle θ , thus q
- $U_{\text{Substrate}} \geq U_{\text{Fe}} - |\mu_n B|$



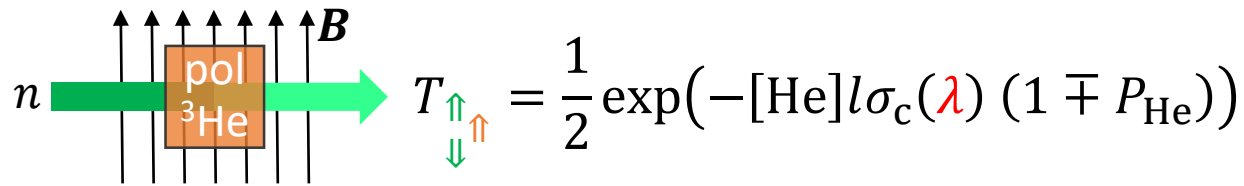
- Strongly reduced λ, θ dependence
- Compact → high magnetizing field



Polarization analysis

^3He spin filters $^3\text{He}(n,p)^3\text{H}$: $\sigma_{\uparrow\downarrow} \gg \sigma_{\uparrow\uparrow}$

- $\sigma_{c,0} = 5333(7)$ barn, $\sigma_{\uparrow\downarrow}/\sigma_{c,0} = 1.010(32)$



- For unpolarized beam: $O(\lambda) = \frac{0.0733 p l \lambda}{\text{bar cm \AA}}$

➤ $P_n(\lambda) = \tanh(O(\lambda)P_{\text{He}})$

➤ $T_n(\lambda) = \exp(-O(\lambda)) \cosh(-O(\lambda)P_{\text{He}})$

- Relaxation of hyperpolarized ^3He polarization:

➤ $P_{\text{He}}(t) = P_{\text{He}}(0) \exp\left(-\frac{t}{t_0}\right)$

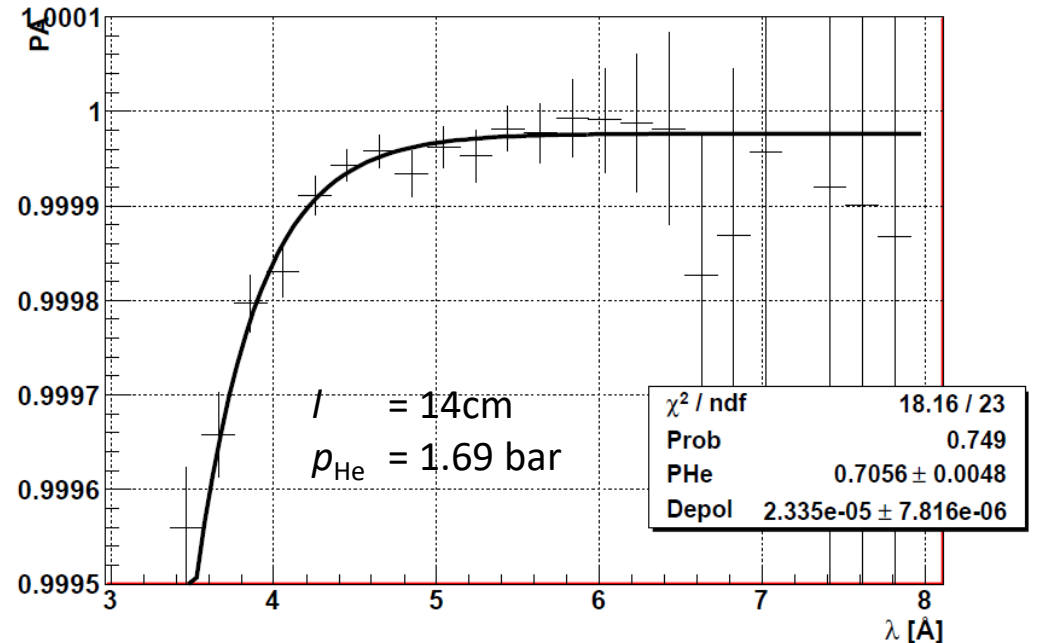
- **In-situ flipping of ^3He spin** → separation of neutron spin flip efficiency and polarization:

$$PA = \frac{n_{\uparrow\uparrow} - n_{\uparrow\downarrow}}{n_{\uparrow\uparrow} + n_{\uparrow\downarrow}}, \quad 2f - 1 = \frac{n_{\uparrow\uparrow} - 2n_{\downarrow\uparrow} + n_{\uparrow\downarrow}}{n_{\uparrow\uparrow} - n_{\uparrow\downarrow}}$$

Performance

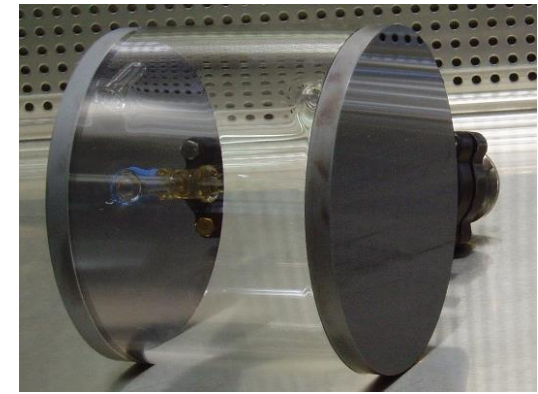
- ~Angle-independent

- $P_n \xrightarrow{O \rightarrow \infty} 1$. $P_n > 99.99\%$ demonstrated:



C. Klauser, PhD thesis (2013)

- Typical numbers: $P_{\text{He}}(0) > 75\%$, $t_0 > 400 \text{ h}$, P_{He} loss per in-situ ^3He spin flip: $\lesssim 10^{-5}$



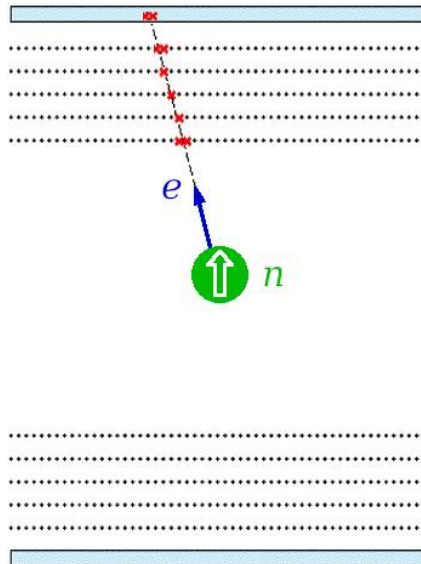
Precise detector solid angle?

Infinitely small and far away

- No integration needed:

$$\cos(\angle(\mathbf{P}_n, \mathbf{p}_e)) = 1 \quad (\text{if aligned})$$

- No statistics
- **Approximation:** tracking detector \rightarrow $\cos(\angle(\mathbf{P}_n, \mathbf{p}_e))$ known for each track

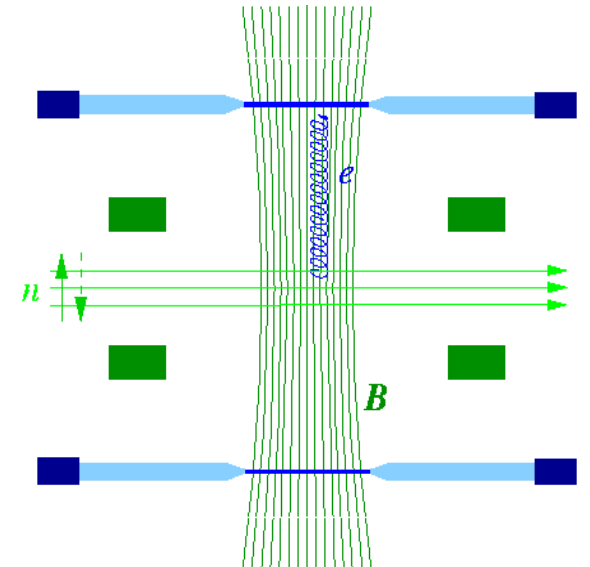


Infinitely large

- Integration = mean over hemisphere:

$$\langle \cos(\angle(\mathbf{P}_n, \mathbf{p}_e)) \rangle_{2\pi} = \frac{1}{2}$$

- Full statistics (but dilution factor 1/2)
- **Realization:** Strong magnetic field



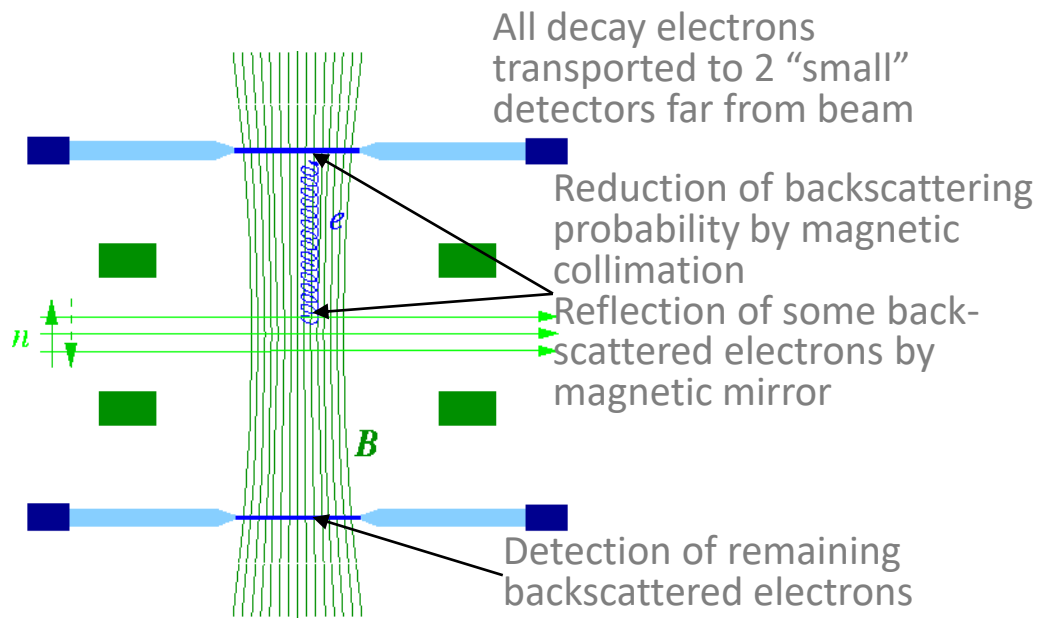
In between \rightarrow Monte Carlo

Requires accurate knowledge of neutron distribution and detector response in space

Neutron beams are large, divergent, inhomogeneous

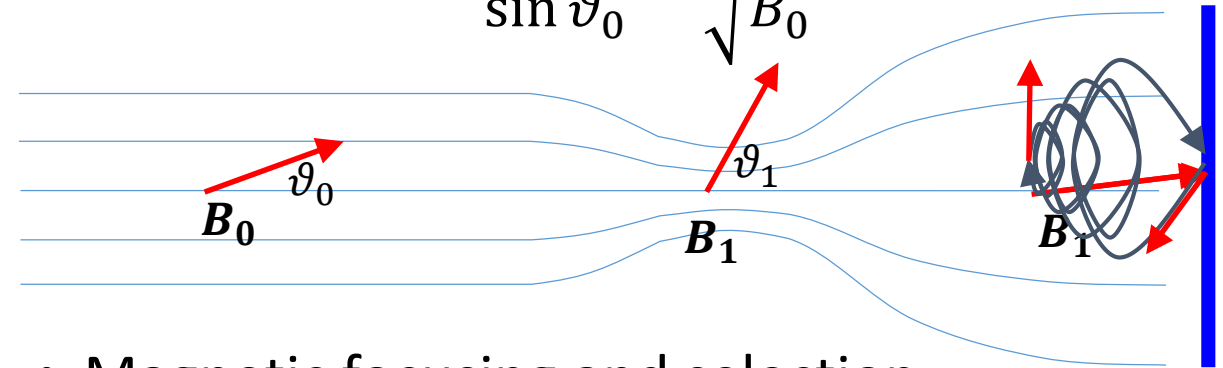
The beauty of (strong) magnetic fields

- Defined solid-angle integration
- Full beam averaging (if large detector)
- Collection of full statistics
- Transport to detectors far away from beam
- Confinement of backscattered particles, too
- Momentum manipulation by **magnetic mirror effect**



Magnetic mirror effect

$$\frac{\sin \vartheta}{\sin \vartheta_0} = \sqrt{\frac{B}{B_0}}$$



- Magnetic focusing and selection:
 $\sin \vartheta_C = \sqrt{B_0/B_1}$
- Magnetic alignment/collimation
 → Reduced backscattering probability
 → Improved resolution of electrostatic filters
- Magnetic mirror → part of backscattered particles reflected

Parameters of the SM, Sensitivities to $\lambda = g_A/g_V$

$$a = \frac{1 - \lambda^2}{1 + 3\lambda^2}$$

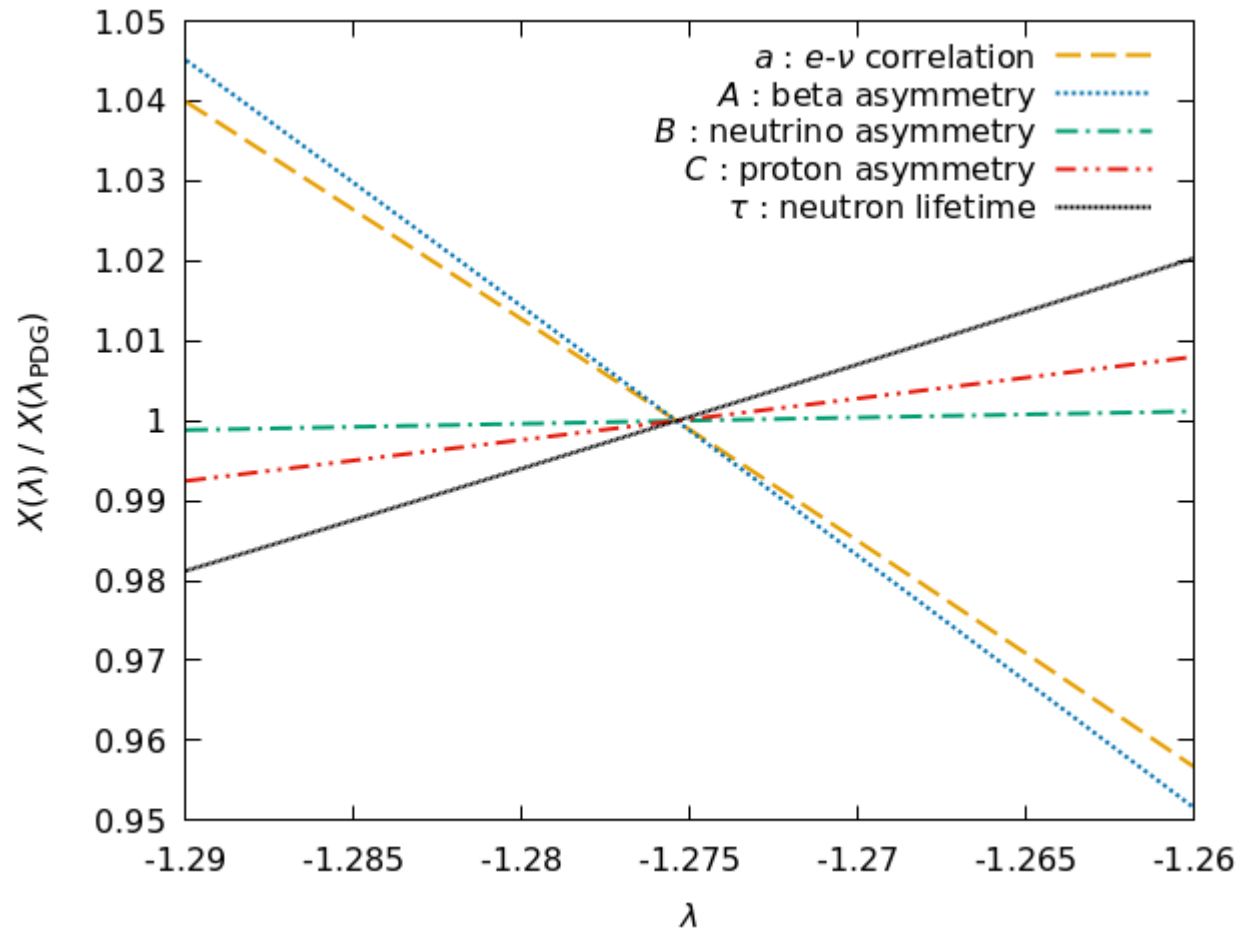
$$A = -2 \frac{\lambda(1 + \lambda)}{1 + 3\lambda^2}$$

$$B = 2 \frac{\lambda(\lambda - 1)}{1 + 3\lambda^2}$$

$$C = x_C(A + B)$$

$$\tau = \frac{4908.6(1.9) \text{ s}}{|V_{ud}|^2(1 + 3\lambda^2)}$$

(Lecture I)



τ and λ necessary to determine SM parameter V_{ud}

- a, A most sensitive for determination of λ
- B, C most suitable to search for new physics

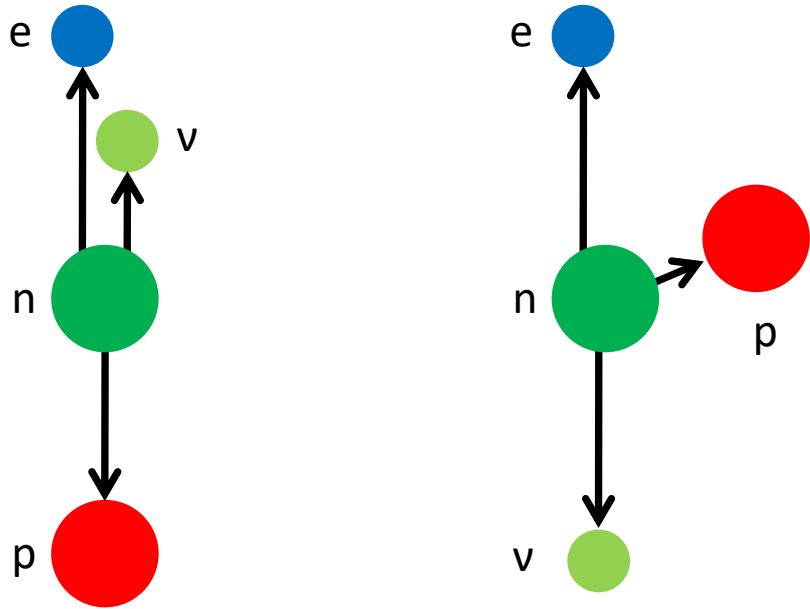
(assuming similar experimental accuracy)

$$a: \quad dW \propto 1 + a \frac{\mathbf{p}_e \mathbf{p}_\nu}{E_e E_\nu}$$

$e-\nu$ asymmetry and proton spectrum

- Correlation as spatial asymmetry:

$$a \propto \frac{n_{\uparrow\uparrow} - n_{\uparrow\downarrow}}{n_{\uparrow\uparrow} + n_{\uparrow\downarrow}}$$

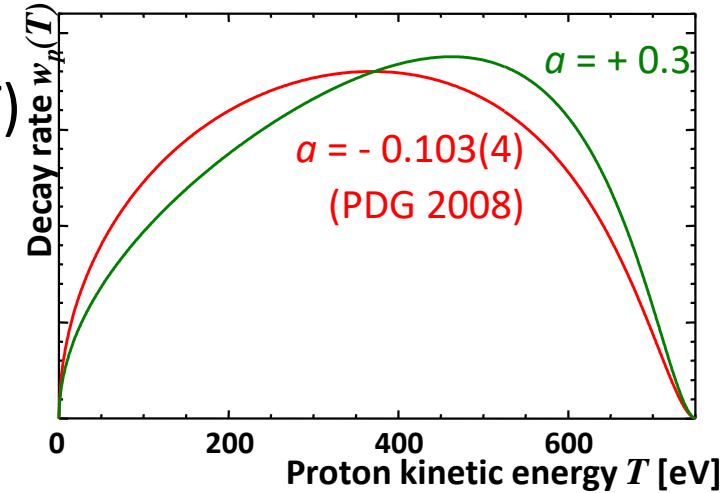


$a > 0$ Proton spectrum shifted to higher energy

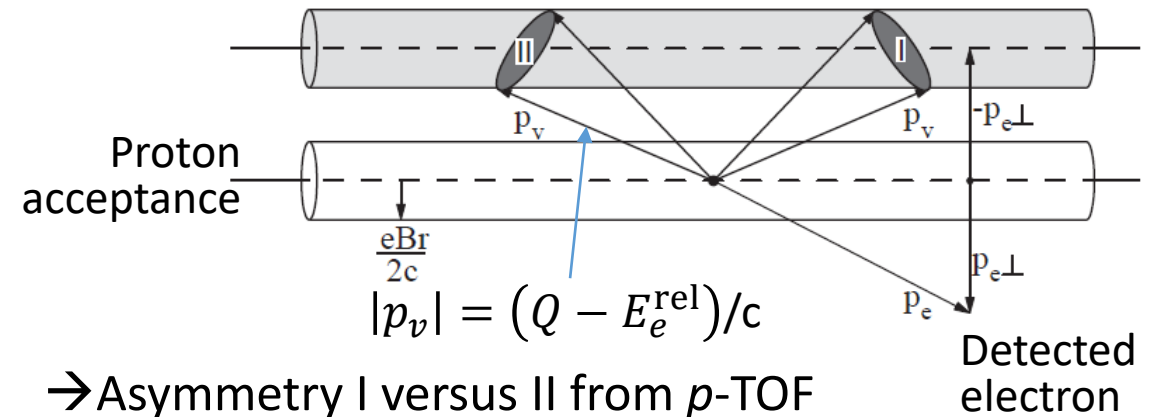
$a < 0$ Proton spectrum shifted to lower energy

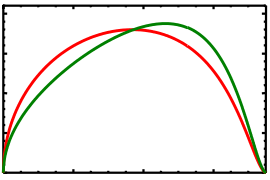
Two principles of measurement

- Proton spectrum (Example aSPECT)



- $e-p$ Asymmetry (example aCORN)

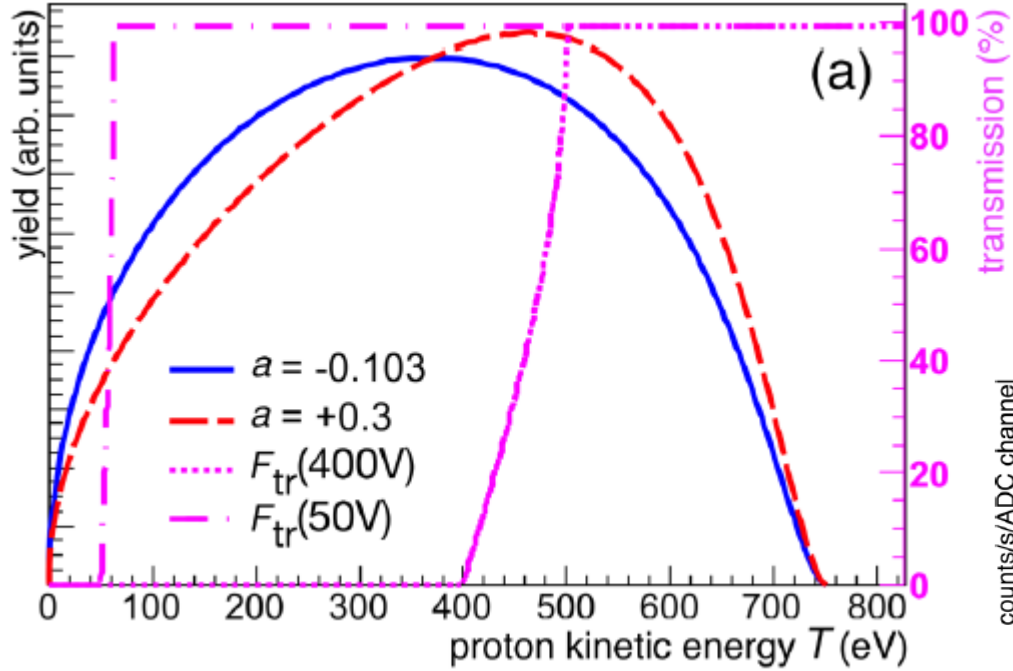




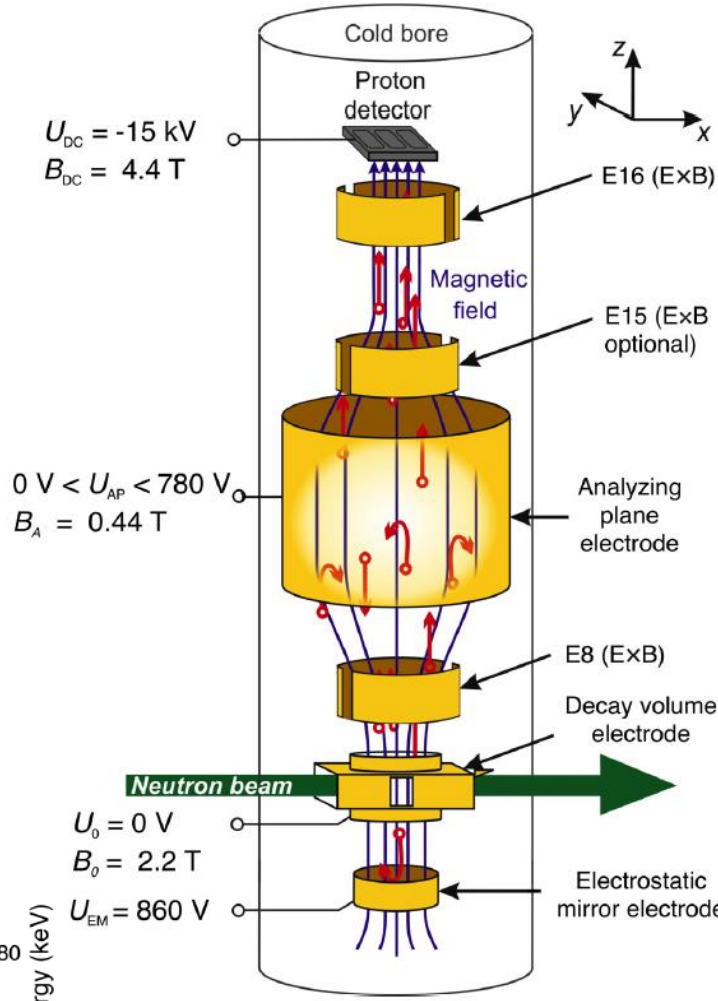
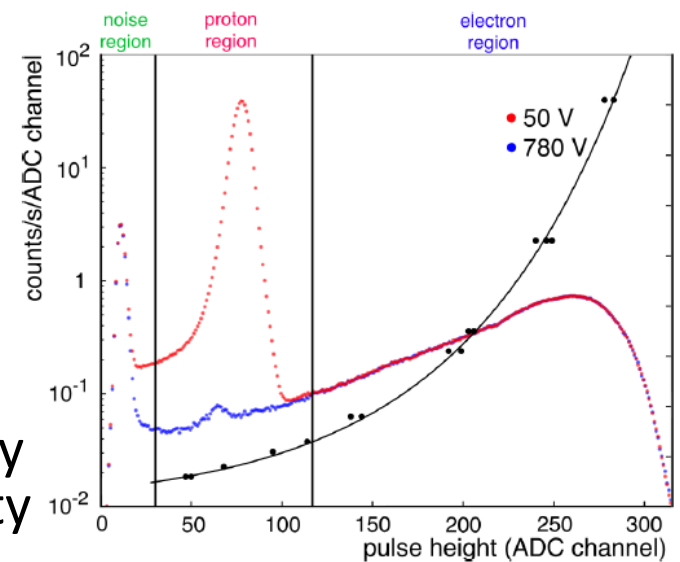
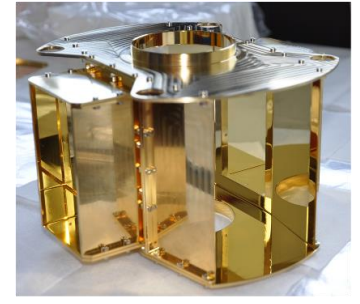
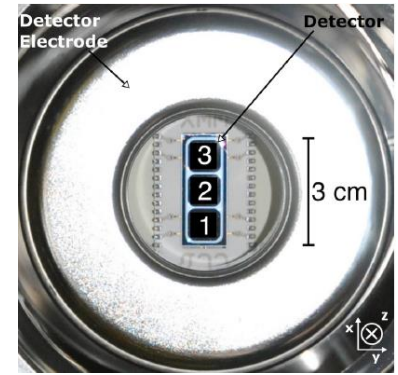
a : aSPECT

Integral proton spectrum from MAC-E filter

- Magnetic Adiabatic Collimation 2.2 T \rightarrow 0.44 T sharpens transmission function of electrostatic filter

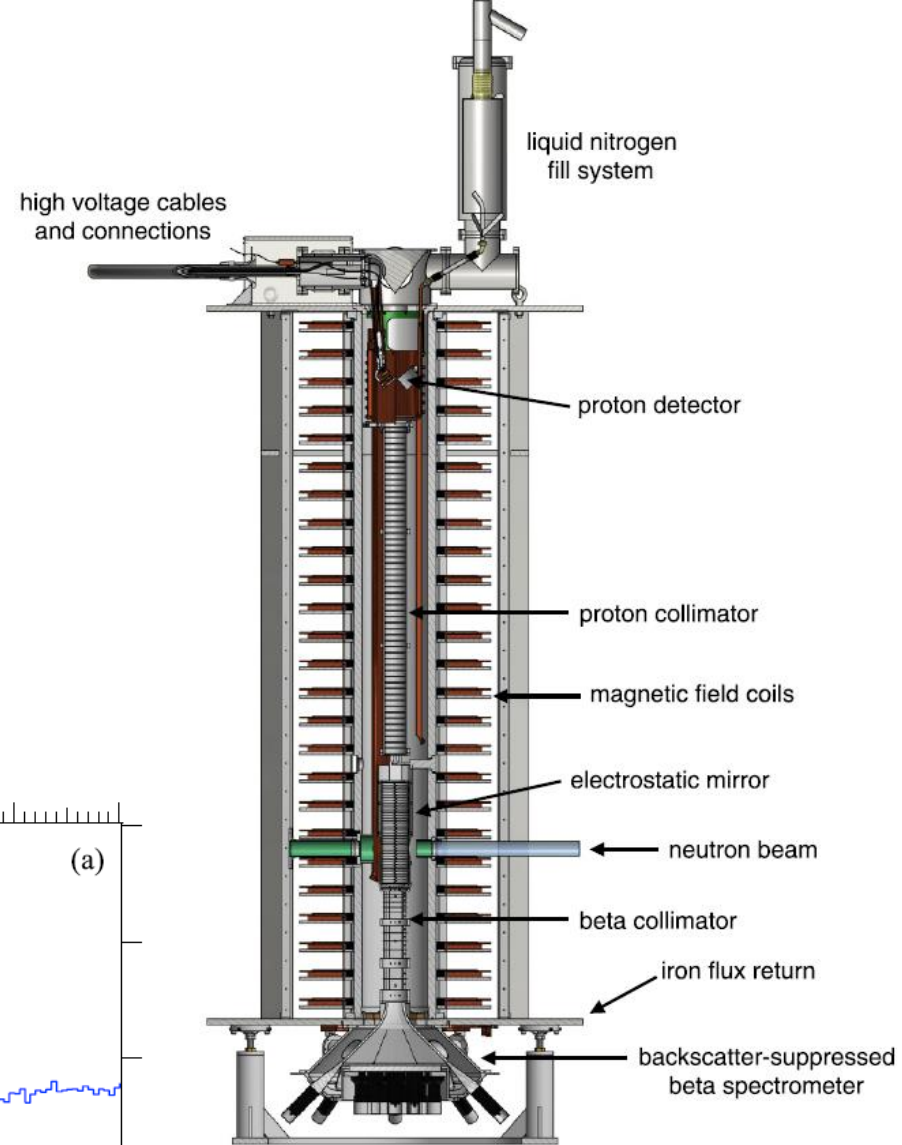
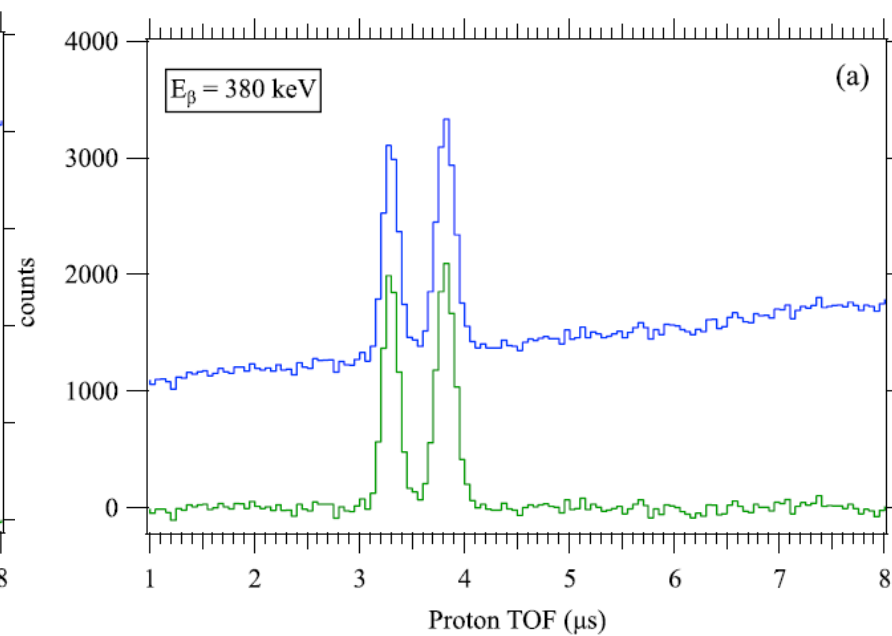
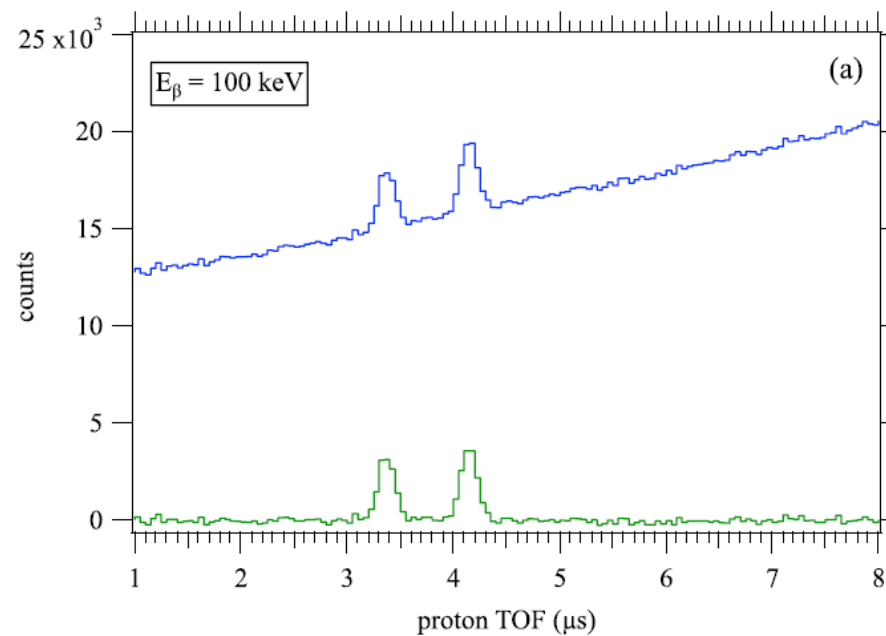
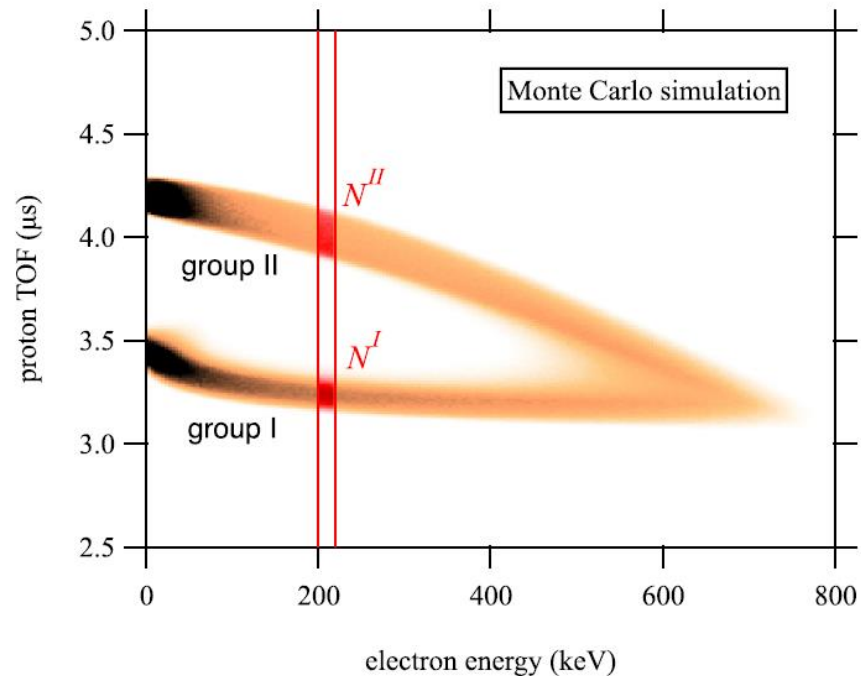
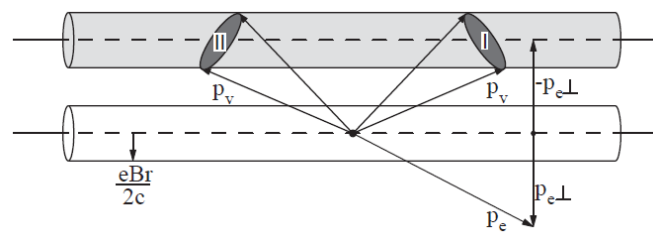


- Stringent requirements on magnetic field, electrodes work functions, detector energy dependence, vacuum, high-voltage stability



$a = -0.10402(82)$ ($b = 0$)
and correlated (a, b) analysis

α : aCORN



$$-0.10859(125^{\text{stat}})(133^{\text{sys}})$$

Darius et al., Phys. Rev. Lett. 119 (2017) 042502

Hassan et al., Phys. Rev. C 103 (2021) 045502

Wietfeldt et al, arXiv:2306.15042

Det1



Det2

Beta asymmetry A

[Burgy et al, Phys. Rev. 120 (1960) 1829]

Early experiments

- Coincidence of electron and proton (needed close to reactor) to reduce background
 - Proton detection by electron multiplication
 - Electron detection by scintillator

→ Small decay volume, low rate

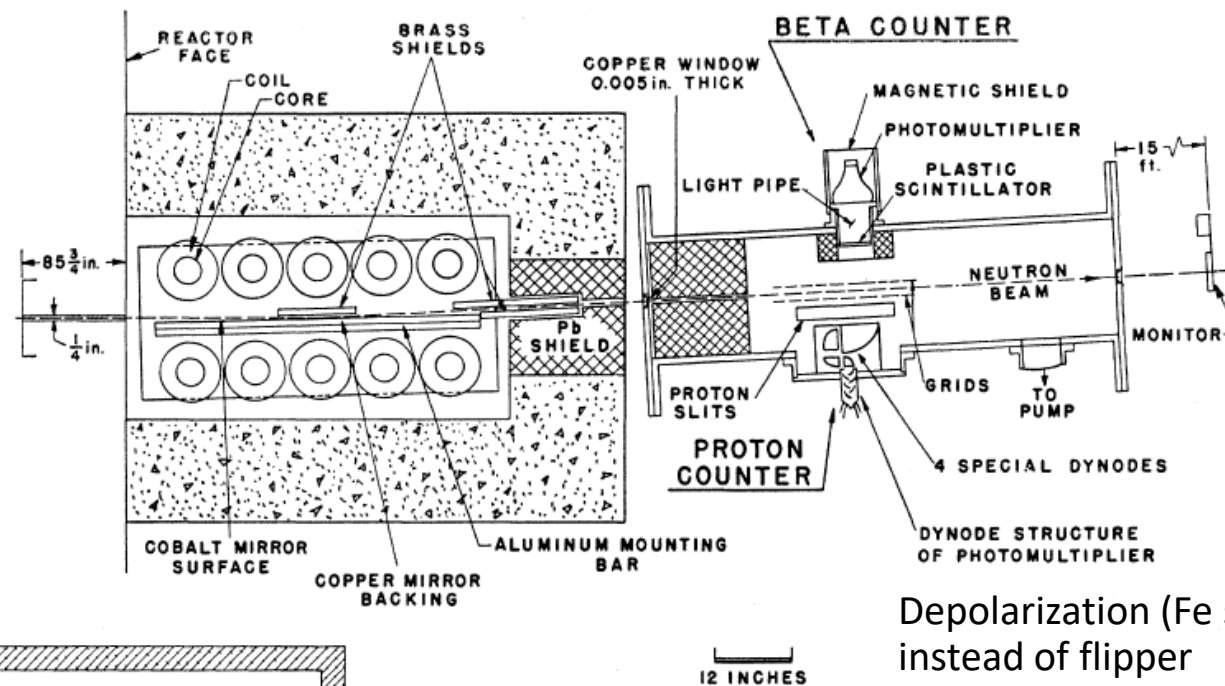
→ Not compatible with 2 symmetric detectors

→ One needs to collect all protons in order to integrate out neutrino:

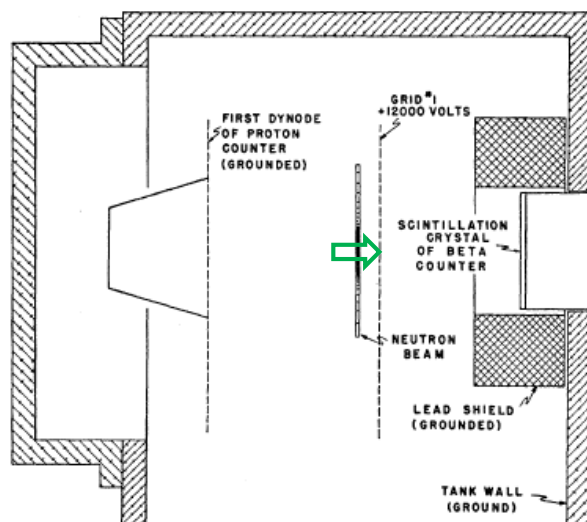
$$dW(\langle \sigma_n \rangle | E_e, \Omega_e, \Omega_\nu) \propto \left\{ 1 + a \frac{p_e p_\nu}{E_e E_\nu} + \frac{\langle \sigma_n \rangle}{\sigma_n} \left(A \frac{p_e}{E_e} + B \frac{p_\nu}{E_\nu} \right) \right\}$$

Incomplete collection → systematics from B and a

Example: First measurement of A (& B, D)



Depolarization (Fe sheet) instead of flipper



Beta energy group	150-780 keV
Observed α	-0.066 ± 0.010
Correction factor for contribution from correlation of neutron spin and proton momentum (antineutrino asymmetry)	1.12 ± 0.03
Correction factor for imperfections of polarization	1.19 ± 0.1
Geometrical correction factor	1.07 ± 0.02
Correction factor for beta velocity, c/\bar{v}	1.20 ± 0.06

$$A = -0.114(19), \frac{\Delta A}{A} = 17\%$$

Det1



Det2

A: PERKEO [1986]

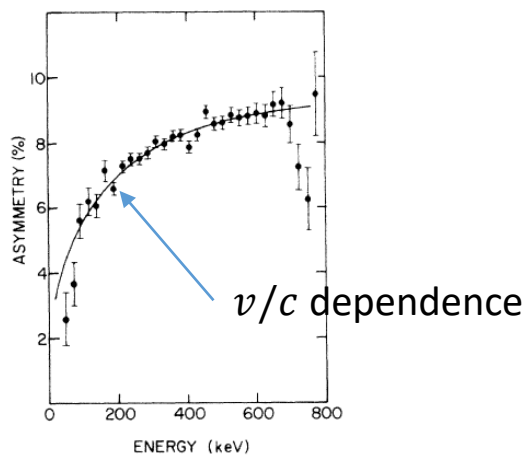
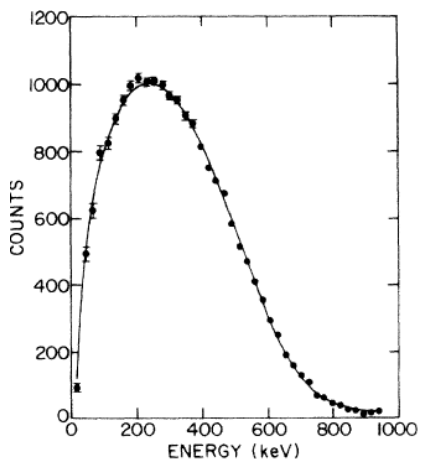
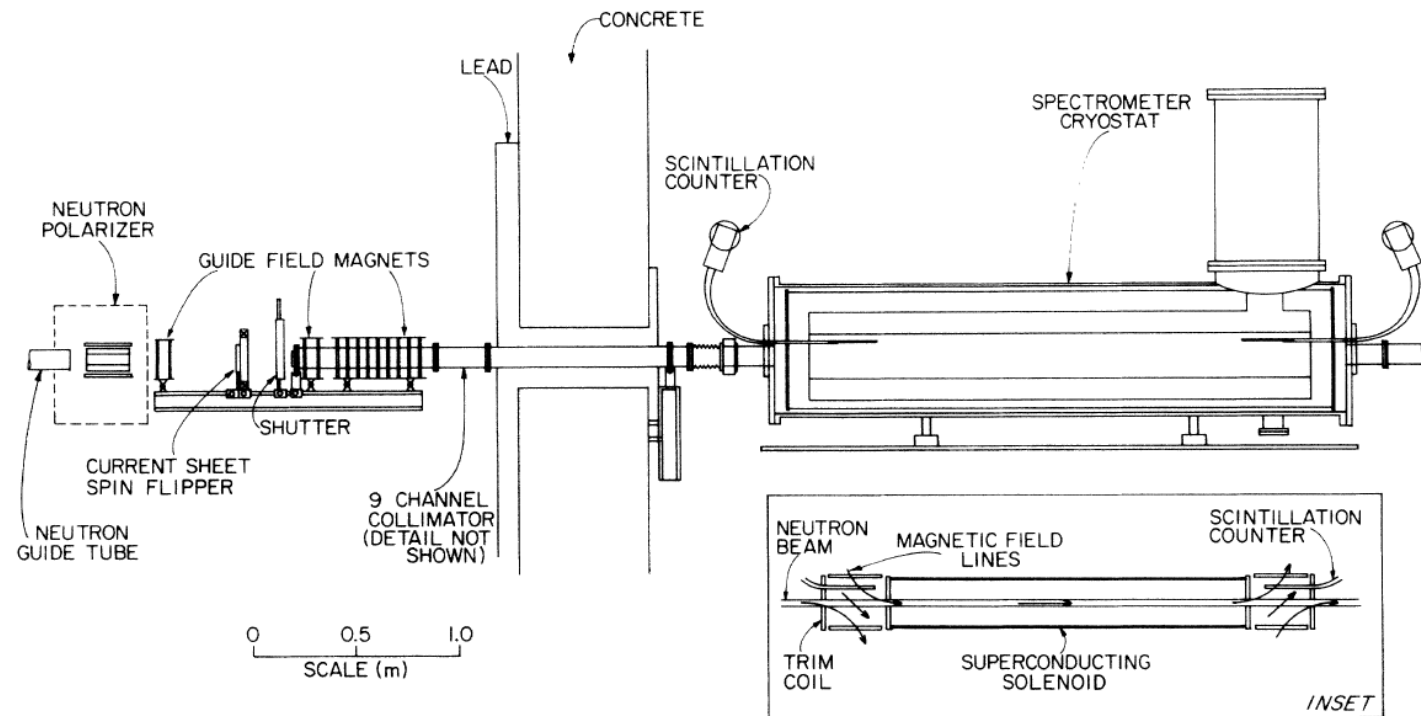
[Bopp et al, Phys. Rev. Lett. 56 (1986) 919]

New possibilities and new concept

- Cold neutron guide of 120 m length
- Supermirror polarizer

PERKEO spectrometer:

- Longitudinal magnetic field (1.5 T, 1.7 m)
 - Strongly enhanced counting rate
 - Strongly improved signal/background
 - Accurate knowledge of solid angle
 - Reconstruction of electron backscatter events after transport to other detector



- Downstream detector difficult to shield
- Field maximum in center, decreases to both sides to avoid traps
 - Magnetic mirror effect: 10% correction on asymmetry
 - (Inverse) magnetic mirror effect reduces backscattering
- Background subtraction with shutter after pol
 - Downstream beam-related BG not included

$$A = -0.1146(19), \frac{\Delta A}{A} = 1.7\%$$

Det1



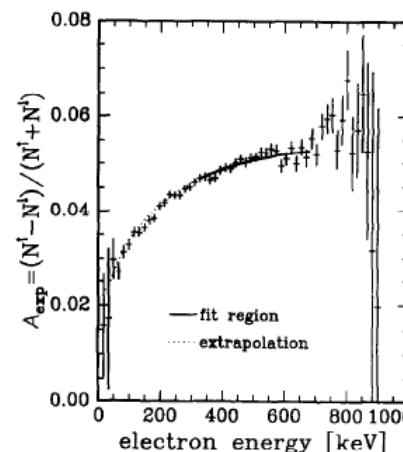
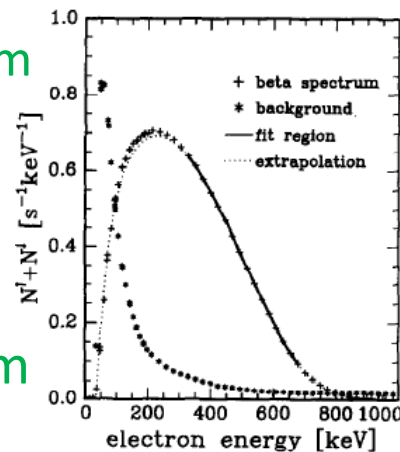
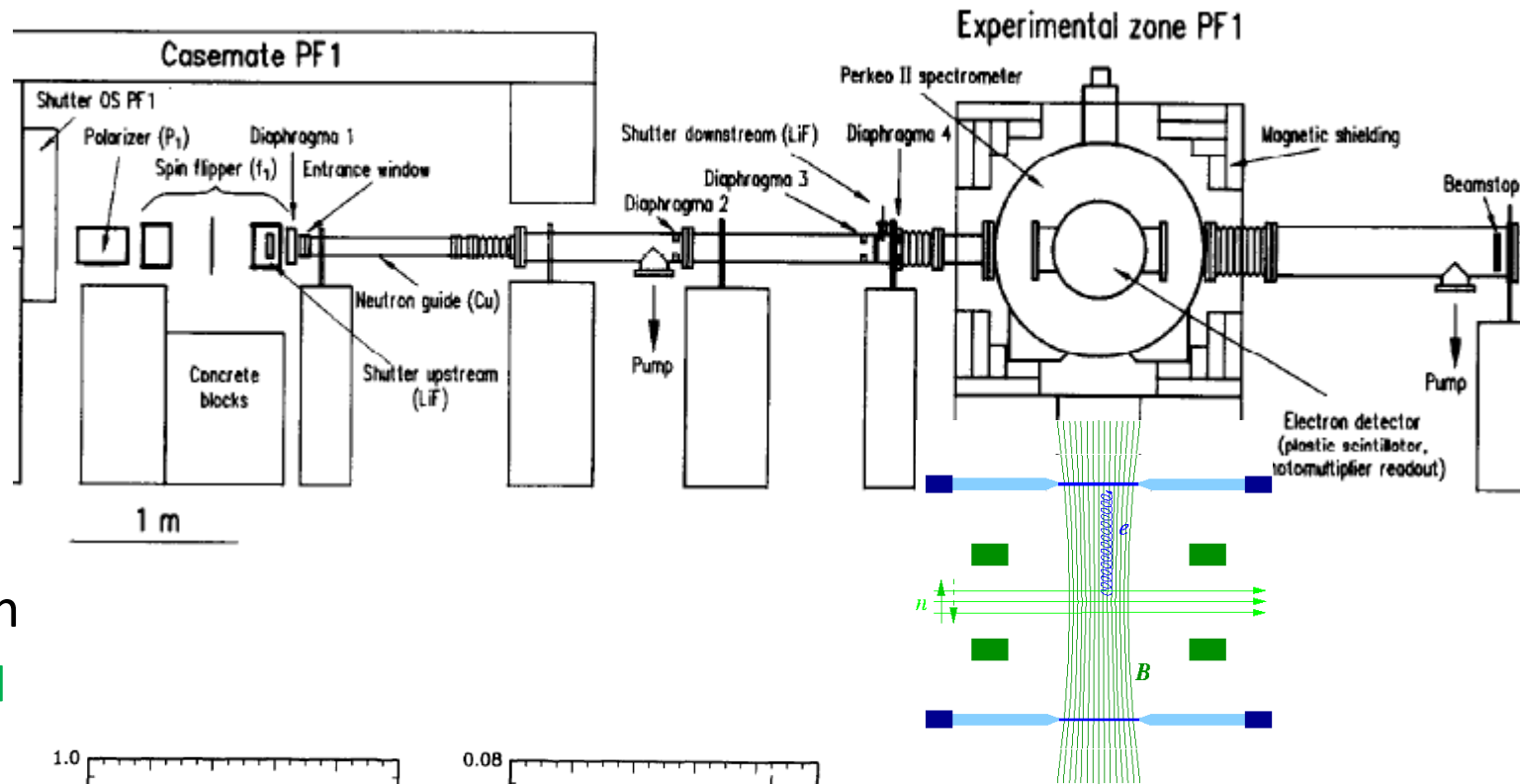
Det2

A: PERKEO II [1997]

[Abele et al, Phys. Lett. B 407 (1997) 212]

Improvements to PERKEO

- **Magnetic field perpendicular** to neutron beam (1.1 T, \varnothing of coils 1 m)
 - Detectors at larger distance to beam
→ Signal/Background in ROI 20:1
 - Decays only close to maximum
→ Reduced magn. mirror effect
- **Two shutters** for background estimation
 - **Upstream shutter** → only environmental background
 - **Downstream shutter** → (enhanced) beam related background
 - **Strong n and γ sources along beam line**
→ same shape as from downstr. shutter (multiple scattering to reach detectors)
→ Extrapolation of background spectrum above beta endpoint into fit region



Effect	correction	error
Polarization	+2.34%	0.75%
Background	+1.55%	0.45%
Detector response	-0.20%	0.25%
Other sys + rad corr	+0.19%	0.10%
Statistics		0.42%

$$A = -0.1189(12), \frac{\Delta A}{A} = 1.0\%$$

Det1



Det2

A: PERKEO II [1997 → 2002 → 2013]

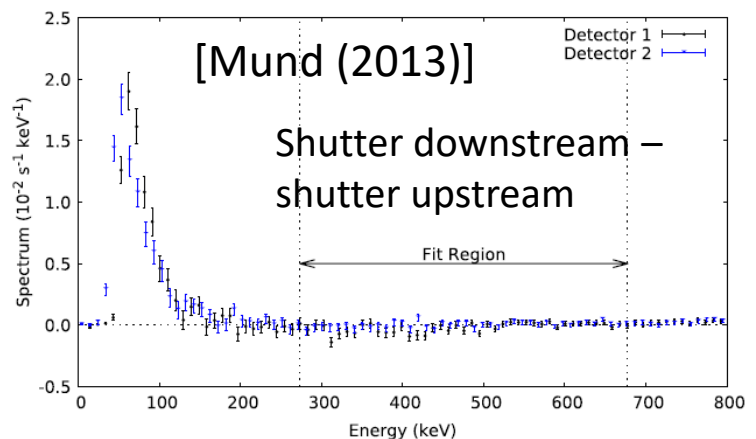
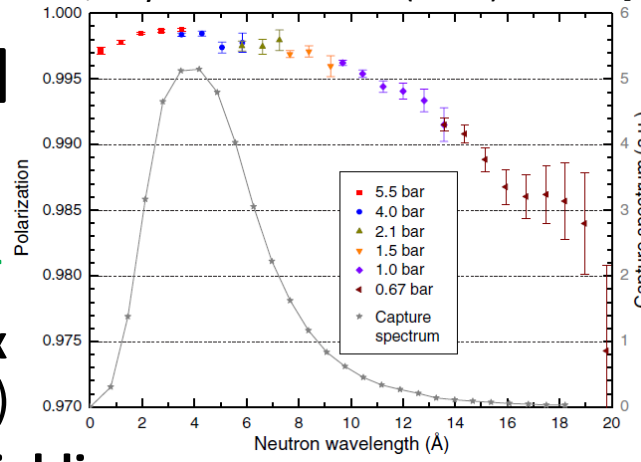
[Abele et al, Phys. Lett. B 407 (1997) 212]
[Reich et al, Nucl. Instr. Meth. A 440 (2000) 535,
Abele et al, Phys. Rev. Lett. 88 (2002) 211801]
[Mund et al, Phys. Rev. Lett. 110 (2013) 172502]

Improvements [1997] → [2002]

- **Cutter for long wavelengths (>13Å)**
 - Suppression of lowly polarized neutrons
- **“Horse” for polarization measurement, non-depolarizing chopper**
 - Separately benchmarked against ³He spin filter and polarized proton spin filter
- **Improved beam line and shielding**
 - Beam stop further away
 - Removal of scattered neutrons
 - Sg/beam-related Bg improved by factor 3

Improvements [2002] → [2013]

- **X-SM polarizer, ³He spin filters**
 - Strongly reduced spatial and λ_n dependence, correction and error
- **New beam line PF1B, 4 × higher flux**
 - Part traded for systematics (X-SM)
- **Further improved beam line and shielding**
 - Sg/beam-related Bg improved by factor 8



	[1997]		[2002]		[2013]	
	Cor [%]	Err [%]	Cor [%]	Err [%]	Cor [%]	Err [%]
Polarization	+2.34	0.75	+1.4	0.31	+0.30	0.14
Background	+1.55	0.45	+0.5	0.25	+0.10	0.10
Detector response	-0.20	0.25	-0.24	0.25	-0.13	0.26
Other systematics	+0.10	0.10	+0.29	0.17	-0.06	0.02
Total systematics		0.91		0.51		0.31
Radiative cor.	+0.09	0.01	+0.09	0.05	-0.11	0.05
Statistics		0.42		0.45		0.38
Total error		1.0		0.68		0.49
A	-0.1189(12)		-0.1189(7)		-0.11972(+53/-65)	

Det1

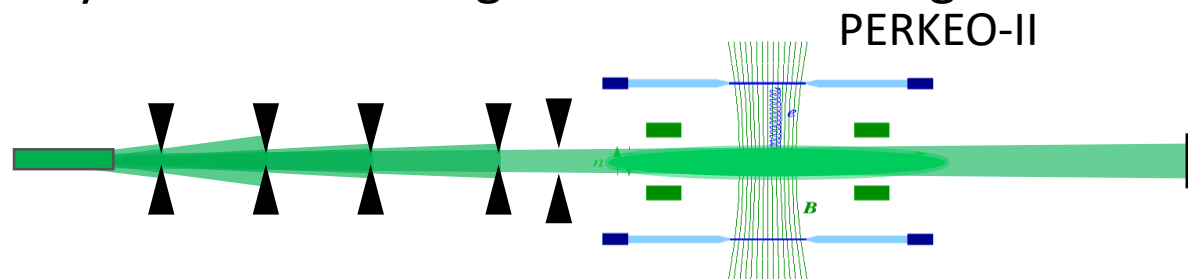


Det2

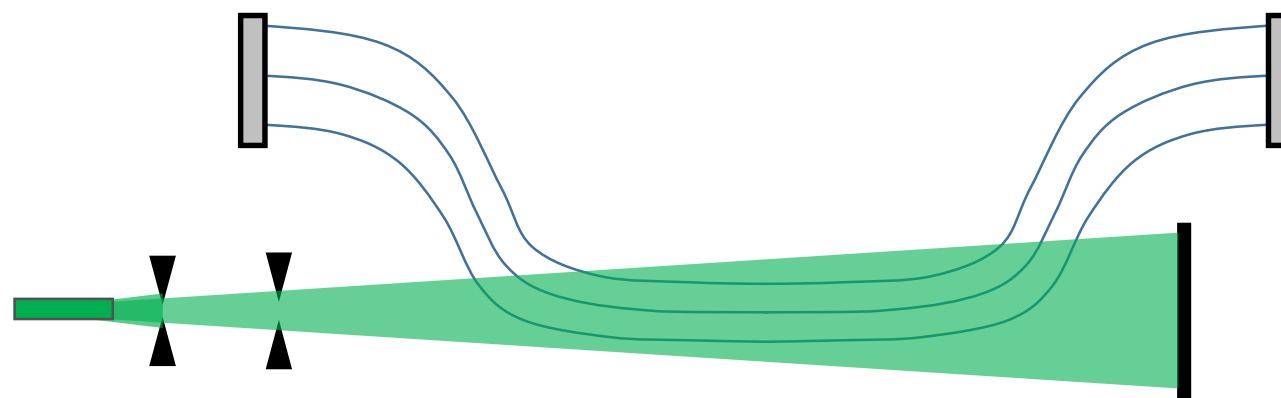
A: PERKEO III

[Märkisch et al, Phys. Rev. Lett. 122 (2019) 242501,
Märkisch et al, Nucl Instr. Meth. A 611 (2009) 216]

- PERKEO II finally limited by statistics. Strong cut in beam divergence to minimize background



- **PERKEO III**: Accept full beam divergence, long decay volume \rightarrow Factor 100 in event rate



- Large beam \rightarrow can accept large gyration radii, lower magnetic field (160 mT), normal conducting
- Detectors can be placed far from beam compared to PERKEO I. However, larger area detectors, downstream detector difficult to shield

Det1

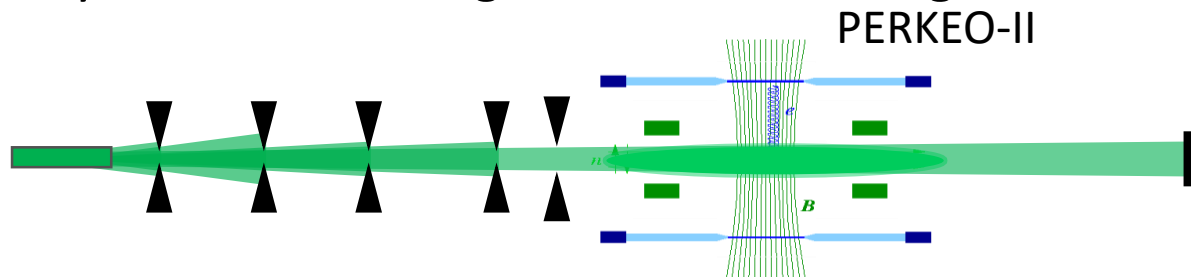


Det2

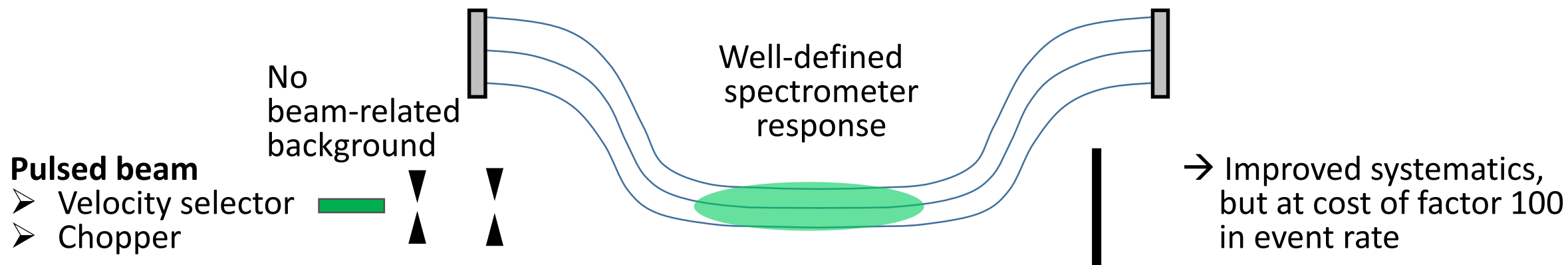
A: PERKEO III

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- **PERKEO III:** Accept full beam divergence, long decay volume \rightarrow Factor 100 in event rate



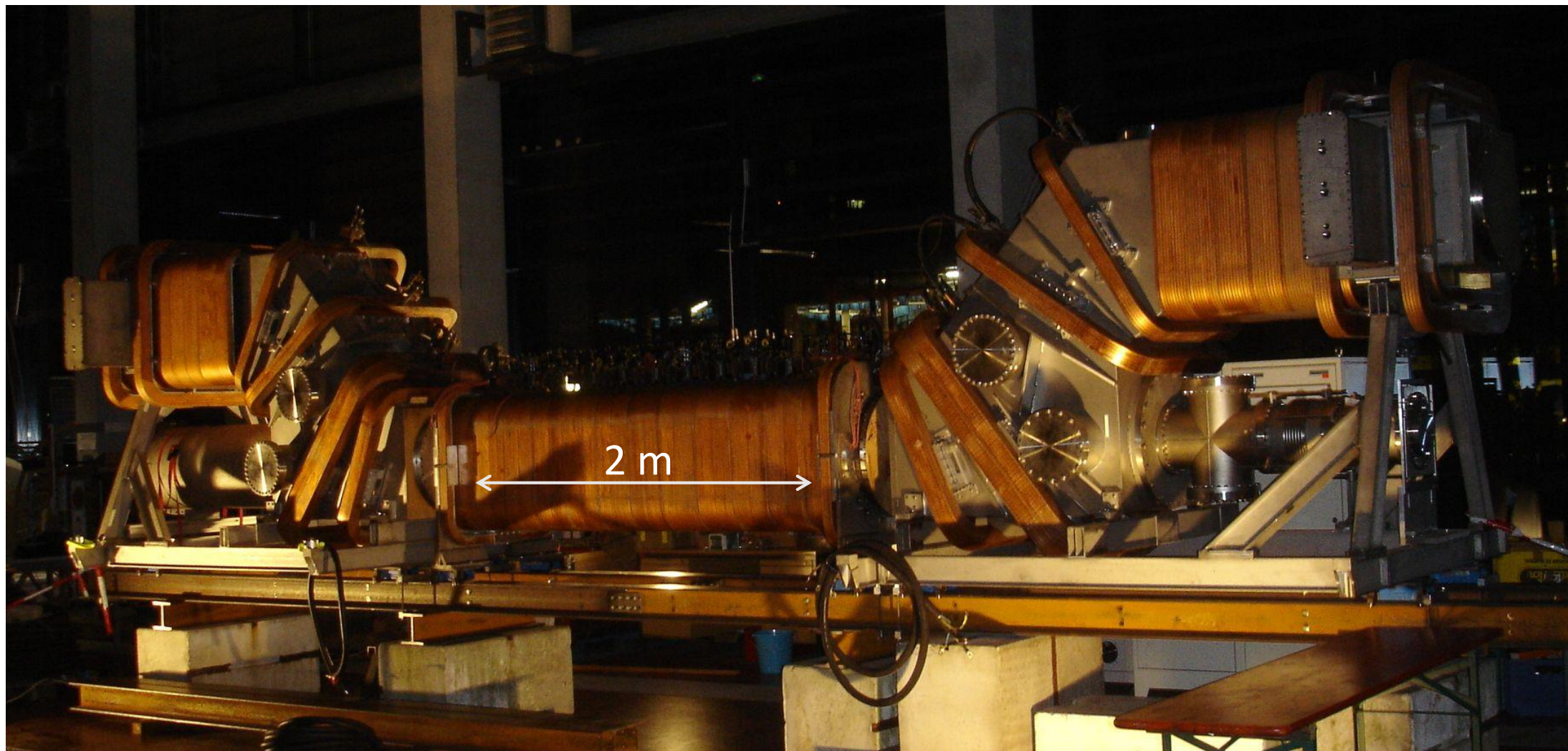
- Large beam \rightarrow can accept large gyration radii, lower magnetic field (160 mT), normal conducting
- Detectors can be placed far from beam compared to PERKEO I. However, larger area detectors, downstream detector difficult to shield

Det1



Det2

A: PERKEO III



Det1

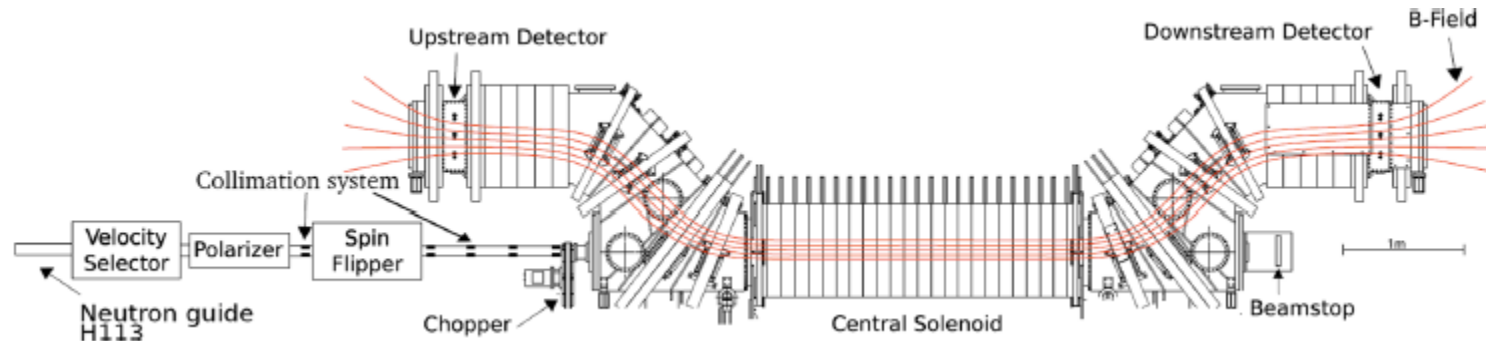


Det2

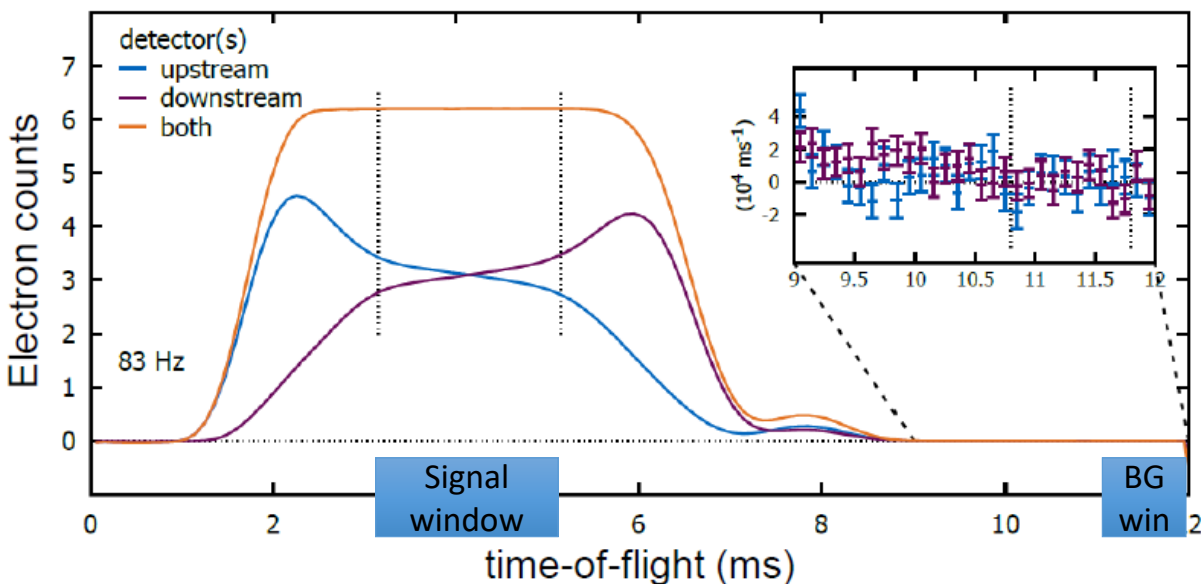
A: PERKEO III

[Märkisch et al, Phys. Rev. Lett. 122 (2019) 242501]

- **Almost monochromatic beam** → X-SM polarizer not needed, only single bender
 ➤ Polarization analysis with opaque ^3He spin filters, exact mapping of full beam
- **Pulsed beam suppresses beam-related background**
- **Improved detector homogeneity**
- **Blind analysis:** Polarization, Asymmetry and Mirror effect analyzed by independent people, combined only at the end

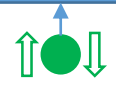


- **Longitudinal field** → increased magnetic mirror effect and uncertainty ($0.45 \cdot 10^{-3}$)



	[2013]		[2019]	
	Cor [10^{-3}]	Err [10^{-3}]	Cor [10^{-3}]	Err [10^{-3}]
Polarization	+3.0	1.4	+9.07	0.64
Background	+1.0	1.0	-0.27	0.11
Detector response	-1.3	2.6	-1.32	0.63
Other systematics	-0.6	0.2	+4.61	0.45
Total systematics		3.1		1.03
Radiative cor.	-1.1	0.5	-1.0	0.1
Statistics		3.8		1.40
Total error		4.9		1.74
A	-0.11972⁽⁺⁵³⁾₋₆₅		-0.11985(21)	

Det1

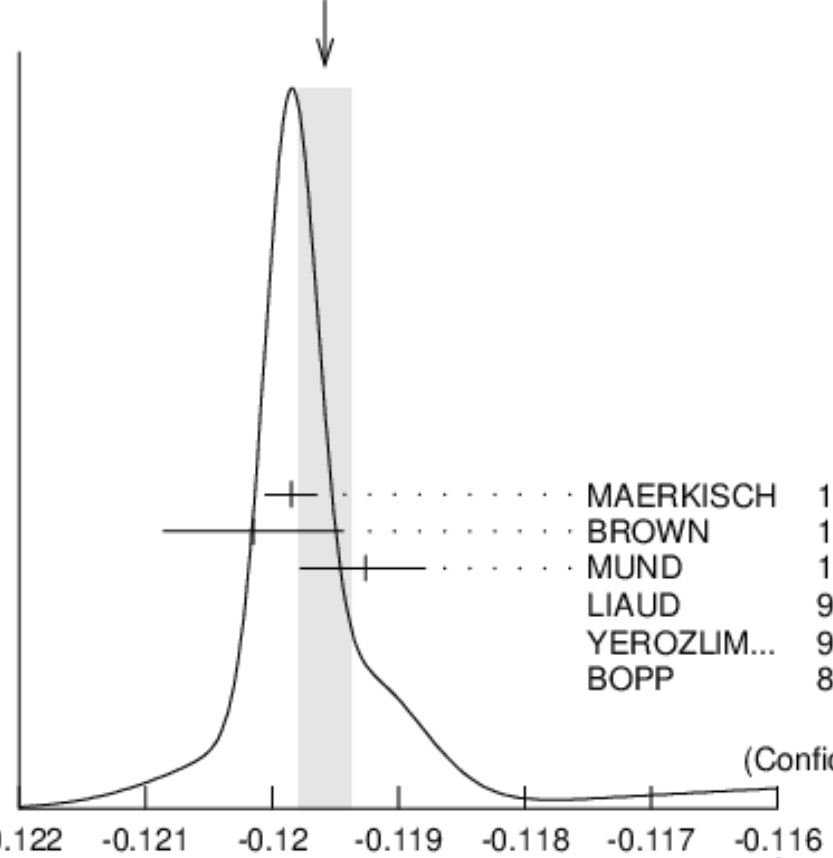


Det2

A: Status

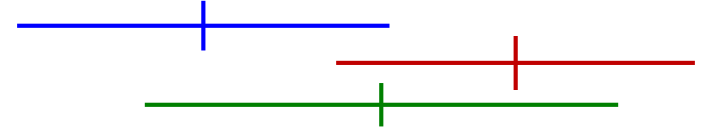
PDG world average of A

WEIGHTED AVERAGE
-0.11958 ± 0.00021 (Error scaled by 1.2)

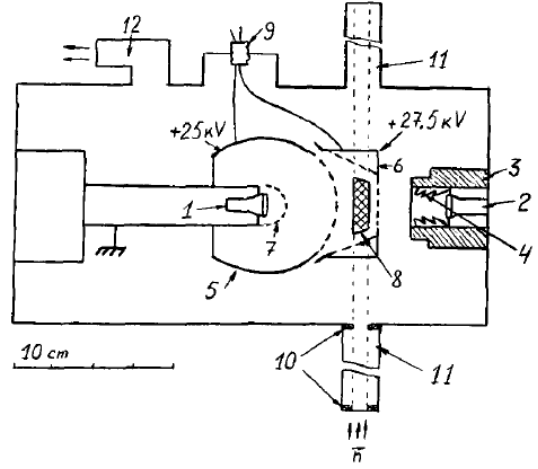


Experiment	Count	Method	χ^2	Notes
MAERKISCH	19	SPEC	1.7	PERKEO III
BROWN	18	UCNA	0.6	<UCNA>
MUND	13	SPEC	0.4	<PERKEO II>
LIAUD	97	TPC		
YEROZLIM...	97	CNTR		
BOPP	86	SPEC		

PERKEO



• Yerozolimsky et al (PNPI): Traditional

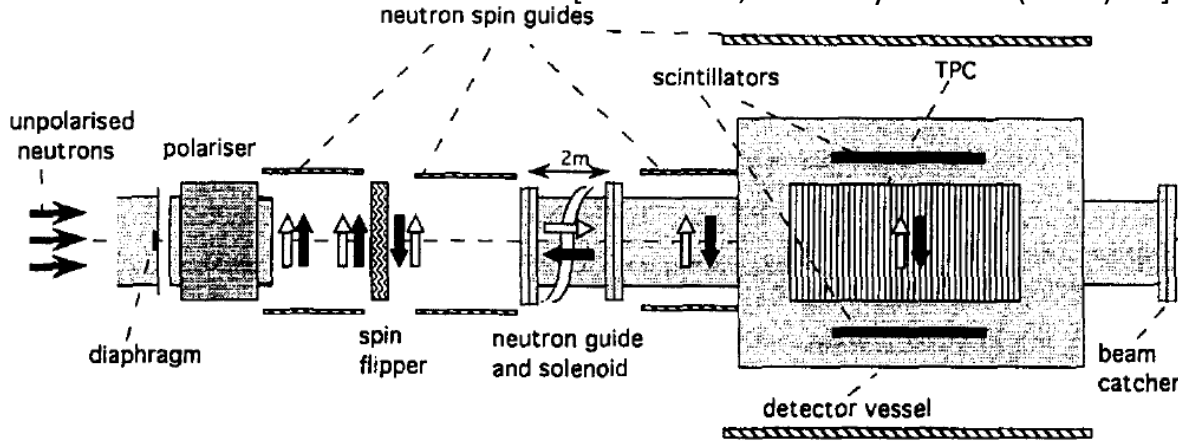


$$A = -0.1135(14), \frac{\Delta A}{A} = 1.2\%$$

[Erozolimskii et al,
Phys. Lett. B 263 (1991) 33,
Yerozolimsky et al,
Phys. Lett. B 412 (1997) 240]

• Liaud et al (ILL): TPC $A = -0.1160(15), \frac{\Delta A}{A} = 1.3\%$

[Liaud et al, Nucl Phys. A 612 (1997) 53]



• Brown et al: UCNA → next slide

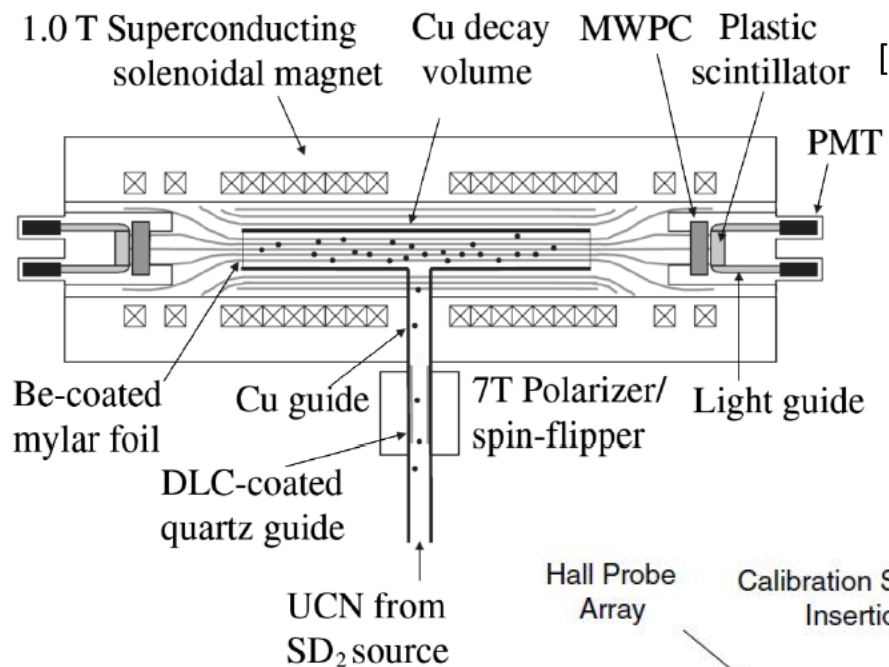
Det1



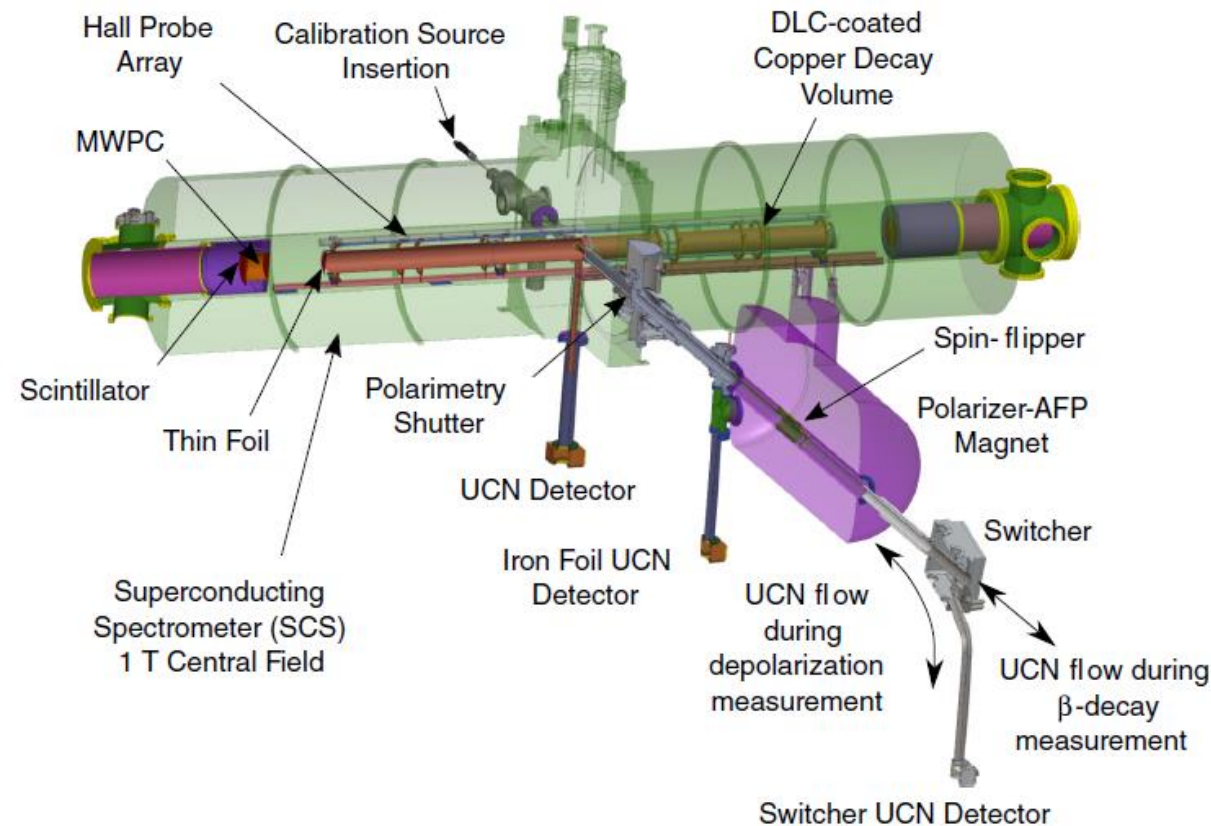
Det2

A: UCNA

- First measurements of any angular correlation with UCN
- **1 T solenoidal spectrometer with 3 m long UCN decay volume**
- **Polarization:**
 - passage through 7 T magnet
 - AFP spin flipper with single-pass spin-flip efficiency > 99.9%
- **Detectors:**
 - **MWPC** (position reconstruction and backscattering identification)
 - **Plastic scintillator** (timing and energy reconstruction)



[Brown et al, Phys. Rev. C 97 (2018) 035505]
 [Mendenhall et al, Phys. Rev. C 87 (2013) 032501(R)]
 [Plaster et al, Phys. Rev. C 86 (2012) 055501]
 [Liu et al, Phys. Rev. Lett. 105 (2010) 181803]
 [Pattie et al, Phys. Rev. Lett. 102 (2009) 012301]



Det1



Det2

A: UCNA

[Brown et al, Phys. Rev. C 97 (2018) 035505]

[Mendenhall et al, Phys. Rev. C 87 (2013) 032501(R)]

[Plaster et al, Phys. Rev. C 86 (2012) 055501]

[Liu et al, Phys. Rev. Lett. 105 (2010) 181803]

[Pattie et al, Phys. Rev. Lett. 102 (2009) 012301]

Systematics

Foils at end of UCN decay trap

- affect backscattering and angular acceptance
- Measurements (and MC) with different foils

Calibration

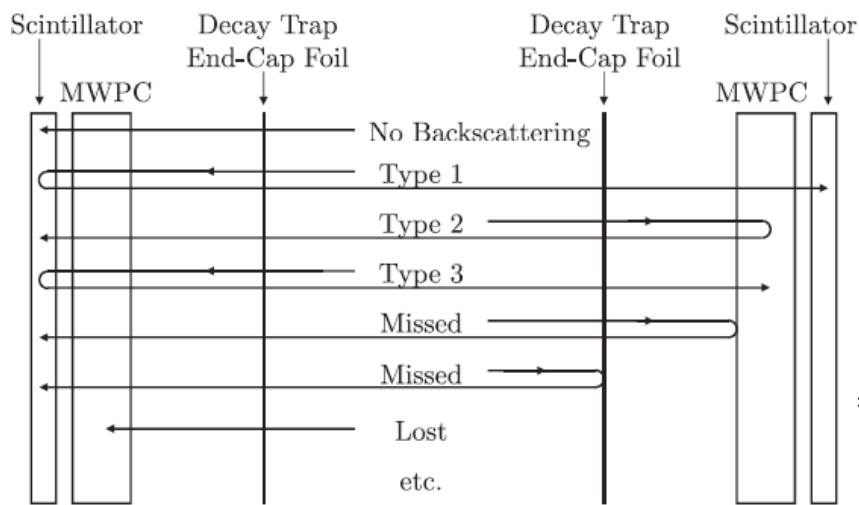
- neutron activated Xe gas with MWPC for homogeneity, conversion electron lines for linearity

Backscattering classification

- Energy cut on MWPC to statistically assign Type 2/3 events to the correct side, reduces Monte Carlo corrections for backscattering events

cos θ correction

- High energy, low pitch angle events more apt to trigger the detectors and carry higher asymmetry information
- Increase measured asymmetry



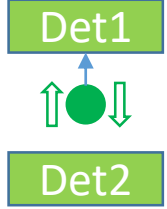
Super-ratio method

- Suppression of spin-dependent trap filling

$$A_{SR} = \frac{1-\sqrt{R}}{1+\sqrt{R}}$$

	% Corr.		% Unc.
	2011–2012	2012–2013	
$\Delta_{\cos\theta}$	-1.53	-1.51	0.33
$\Delta_{\text{backscattering}}$	1.08	0.88	0.30
Energy recon.			0.20
Depolarization	0.45	0.34	0.17
Gain			0.16
Field nonunif.			0.12
Muon veto			0.03
UCN background	0.01	0.01	0.02
MWPC efficiency	0.13	0.11	0.01
Statistics			0.36
	Theory Corrections [11,12,26–29]		
Recoil Order	-1.68	-1.67	0.03
Radiative	-0.12	-0.12	0.05

$$A = -0.12054(44)^{\text{stat}}(68)^{\text{syst}}, \frac{\Delta A}{A} = 0.7\%$$

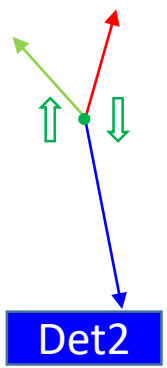


$B:$ $dW \propto 1 + B \frac{\langle \sigma_n \rangle p_\nu}{\sigma_n E_\nu}$

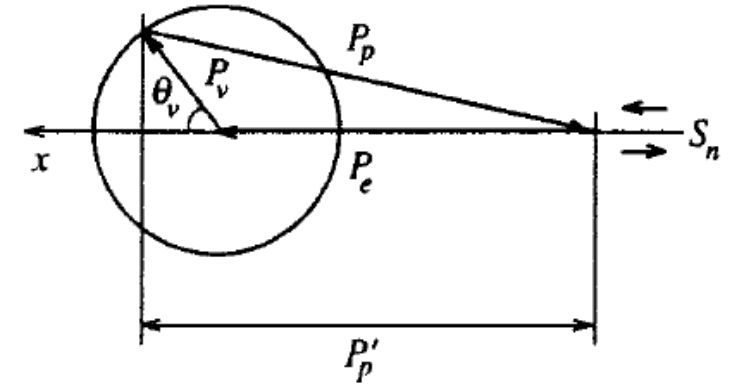
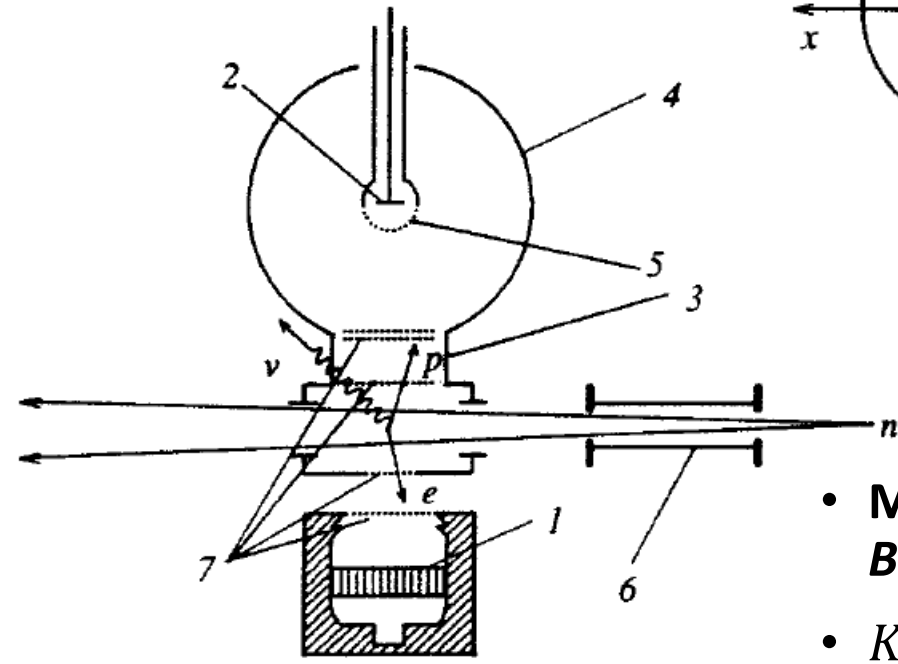
Just the same with ν detector...

Det1

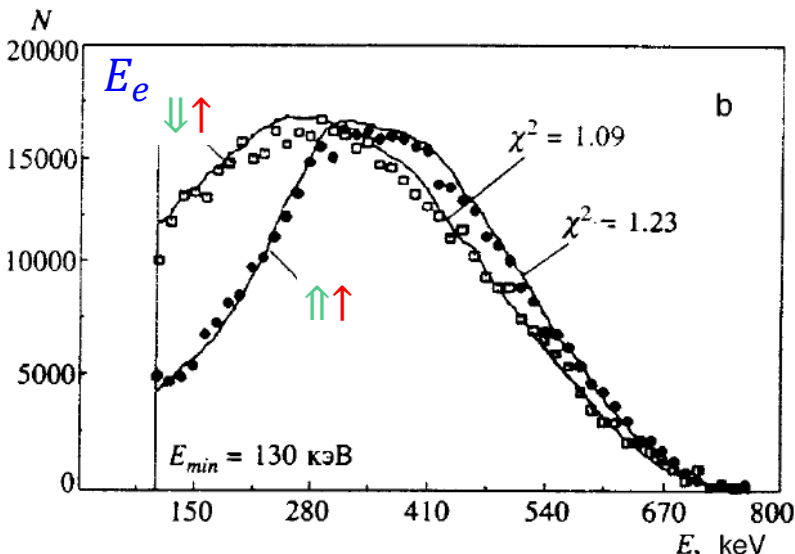
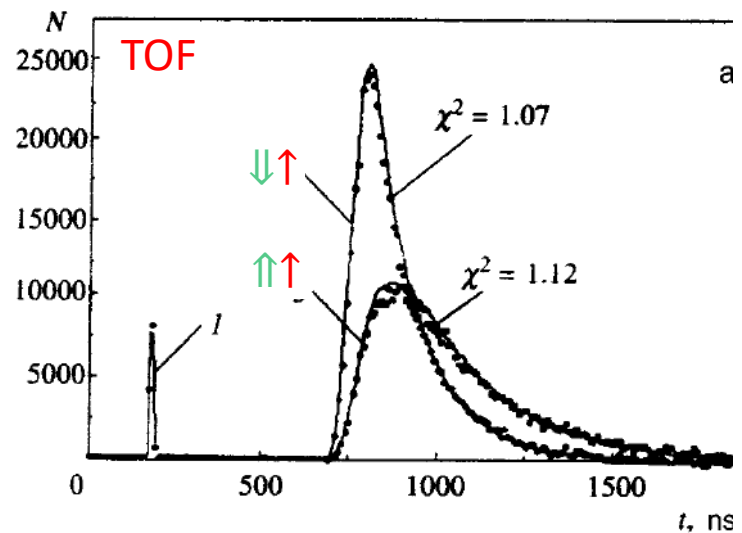
- Opposite e, p detectors: p_ν reconstruction very sensitive to E_e



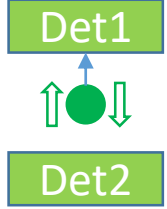
Det2



- Measures combination of B , a and A
- K_B, K_a, K_A to be calculated, a and A from other experiments
- Dominating systematics:
 - Polarization
 - E_e energy resolution



$B = 0.9801 \pm 0.0025^{\text{stat}} \pm 0.0038^{\text{sys}}$



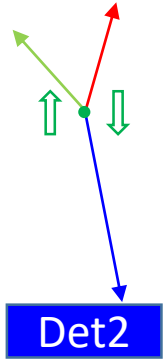
$B:$

$$dW \propto 1 + B \frac{\langle \sigma_n \rangle p_\nu}{\sigma_n E_\nu}$$

Just the same with ν detector...

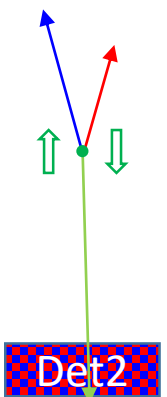
Det1

- **Opposite e, p detectors:** p_ν reconstruction very sensitive to E_e
- Only used for cross-checks in PERKEO II analysis

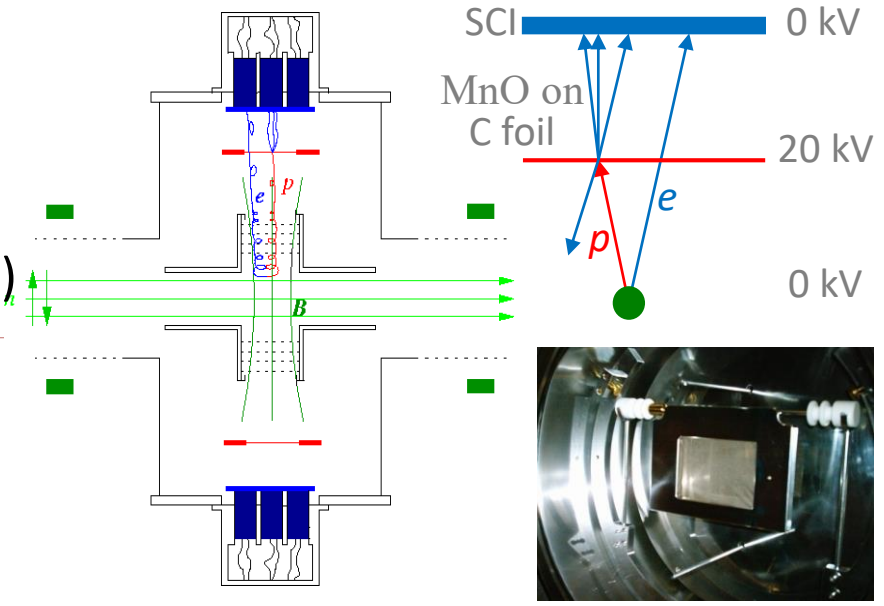
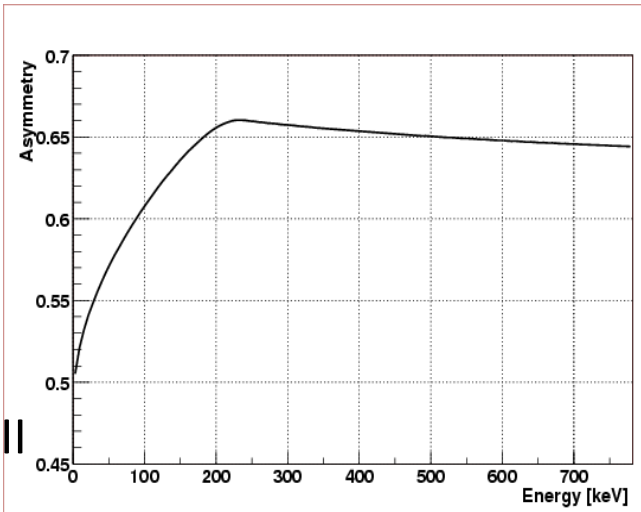
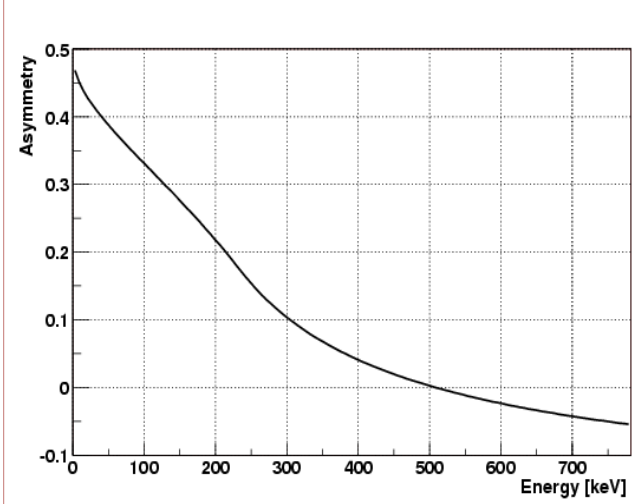


Det1

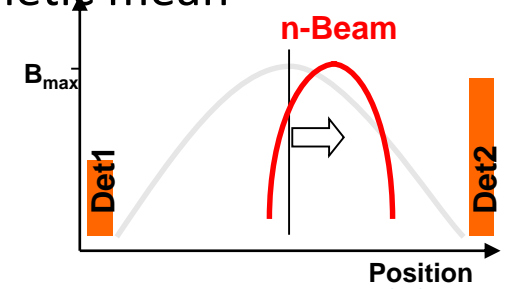
- **e, p in same detector:**
- ➔ p_ν emitted in opposite direction, reconstruction insensitive to E_e
- Result of PERKEO II



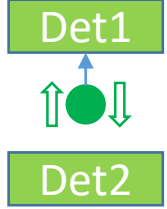
PERKEO II B (with X-SM)



- **A and a** enter (here in fit function)
- Very clean systematics in principle
- **But:** Very different statistical weight of the two detectors (because of high voltage instabilities) → inefficient compensation of beam displacement in arithmetic mean



$$B = 0.9802 \pm 0.0034^{\text{stat}} \pm 0.0036^{\text{sys}}$$

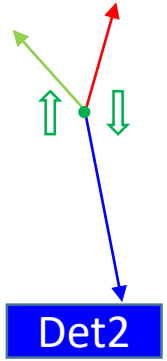


$B:$
$$dW \propto 1 + B \frac{\langle \sigma_n \rangle p_\nu}{\sigma_n E_\nu}$$

Just the same with ν detector...

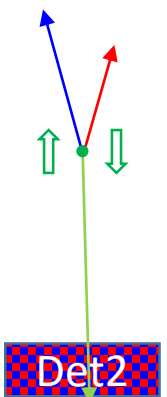
Det1

- **Opposite e, p detectors:** p_ν reconstruction very sensitive to E_e
 - Only used for cross-checks in PERKEO II analysis

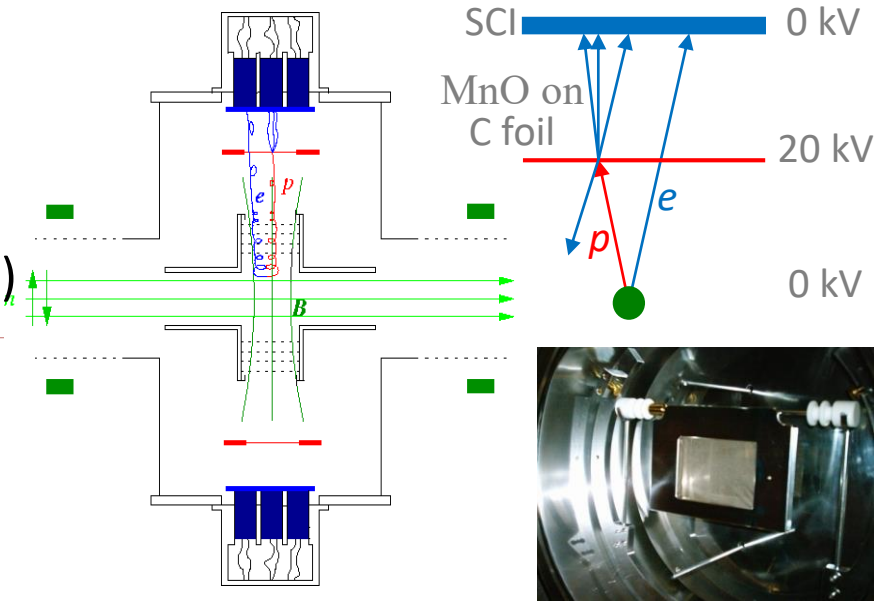
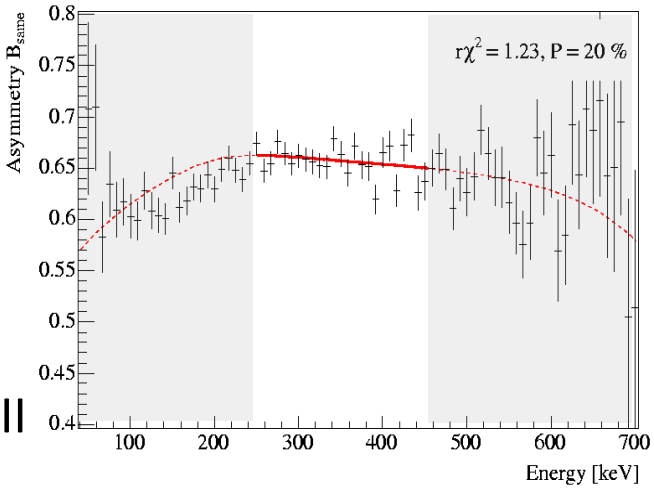
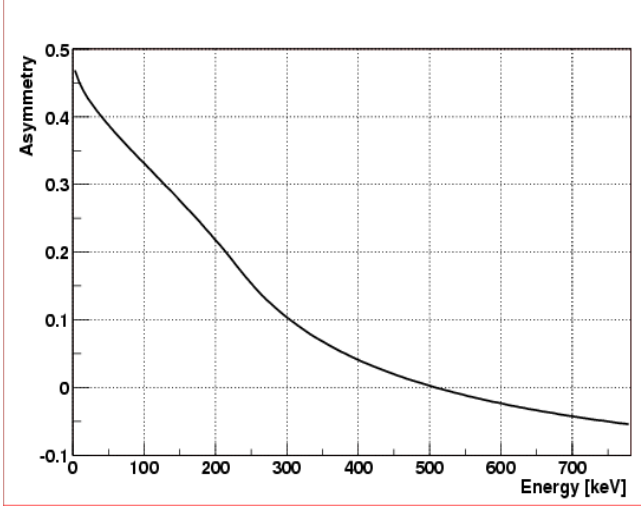


Det1

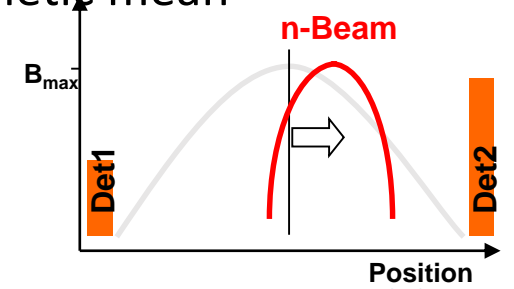
- **e, p in same detector:**
 - ➔ p_ν emitted in opposite direction, reconstruction insensitive to E_e
 - Result of PERKEO II



PERKEO II B (with X-SM)

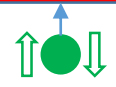


- **A and a enter** (here in fit function)
- Very clean systematics in principle
- **But:** Very different statistical weight of the two detectors (because of high voltage instabilities) ➔ inefficient compensation of beam displacement in arithmetic mean



$$B = 0.9802 \pm 0.0034^{\text{stat}} \pm 0.0036^{\text{sys}}$$

Det1



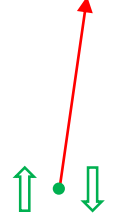
Det2

C:

$$dW \propto 1 + C \frac{\langle \sigma_n \rangle p_p}{\sigma_n p_p}$$

Proton asymmetry parameter C

Det1

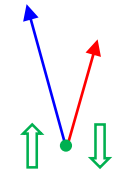


- Not included in alphabet
- Proton detection sufficient, in principle
- Related to A and B by kinematics:
 $C = x_C(A + B), x_C = 0.27484$

Det2

→ Access to B without coincidence measurement

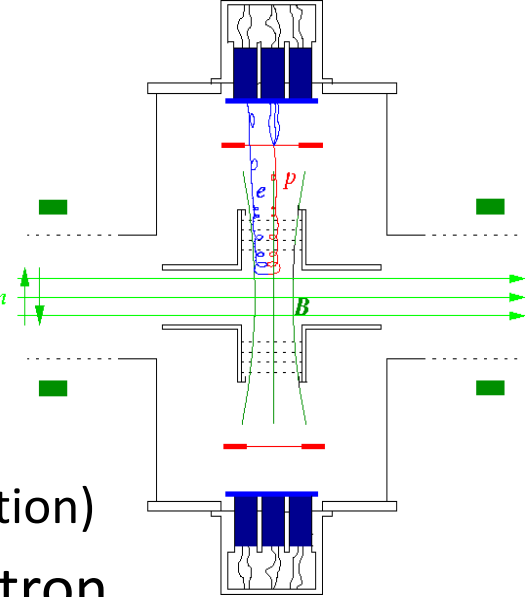
Det1



Det2

So far only: Perkeo II B

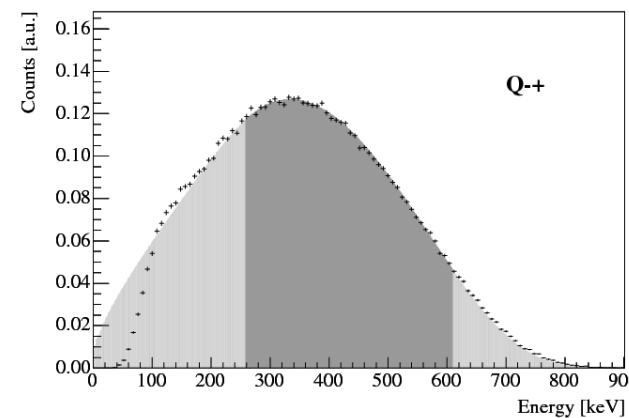
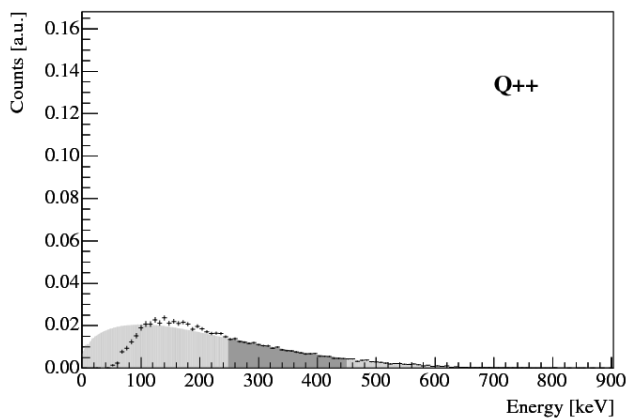
- **Coincident e-p detection:**
 - Distinguish p from e by TOF
 - Suppresses background, too
 - a, A, B enter (here in fit function)
- Need to integrate out electron



$$p_{\uparrow, \downarrow}^1 = \int_{E_e} \left(Q_{\uparrow, \downarrow}^{p1, e1}(E_e) + Q_{\uparrow, \downarrow}^{p1, e2}(E_e) \right) dE_e$$

$$\alpha^1 = \frac{p_{\uparrow}^1 - p_{\downarrow}^1}{p_{\uparrow}^1 + p_{\downarrow}^1}$$

- Proton efficiency drops out but electron energy integral in two different detectors
- Electron threshold + lower cutoff by HV
- Fit theoretical spectra and extrapolate
- Dominating systematics: E_e calibration & resolution
- Only one proton detector used for result



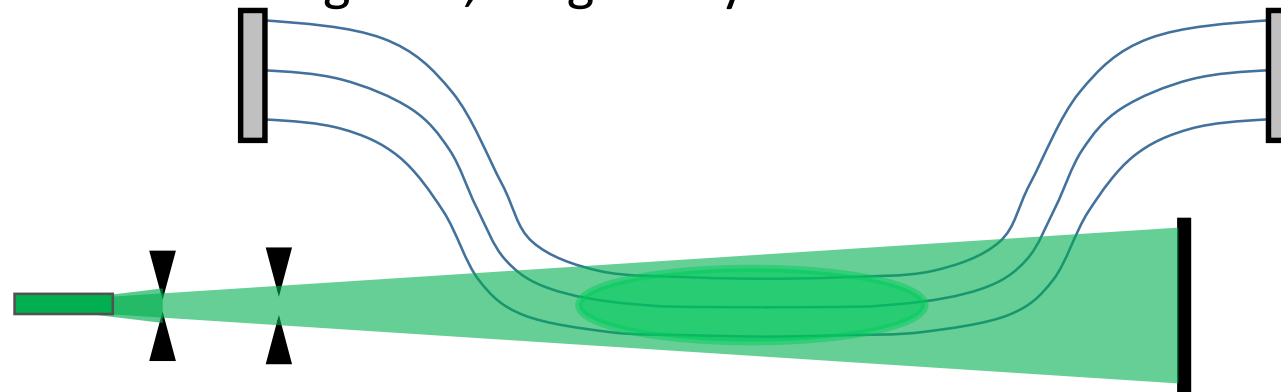
$$C = -0.2377 \pm 0.0010^{\text{stat}} \pm 0.0024^{\text{sys}}$$



: How to go further – PERC

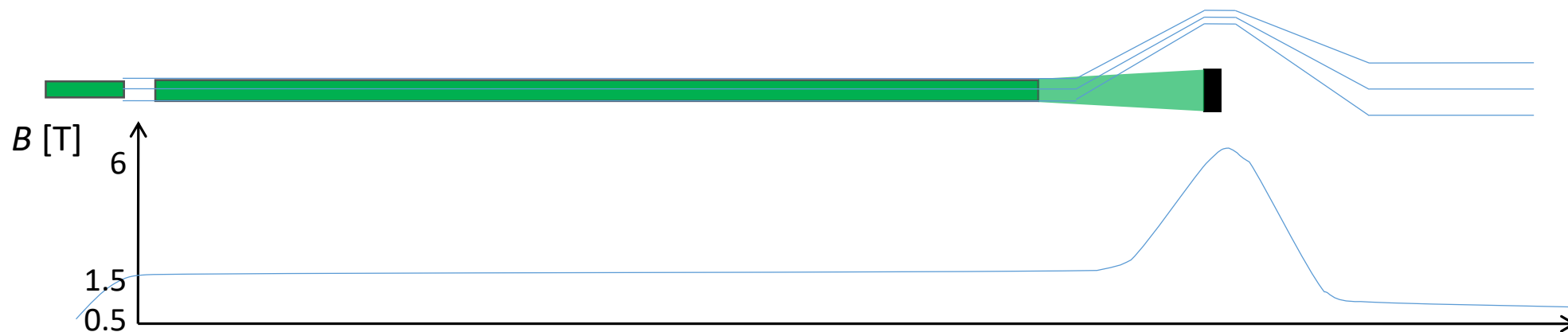
[Märkisch et al, Phys. Rev. Lett. 122 (2019) 242501,
Märkisch et al, Nucl Instr. Meth. A 611 (2009) 216]

- **PERKEO III**: Accept full beam divergence, long decay volume \rightarrow Factor 100 in event rate



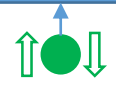
- Yet, beam divergence limits length of decay volume. Large beam, low field \rightarrow Large detectors

\rightarrow **PERC**:

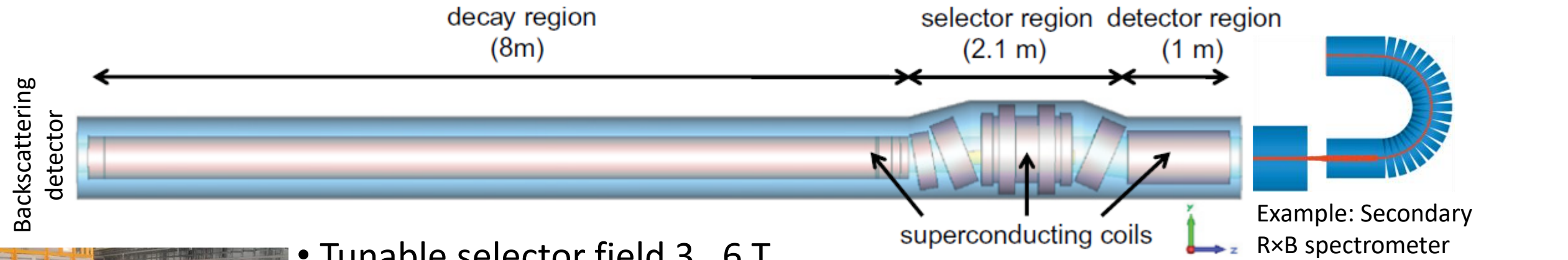


- **Conserve neutron density** by keeping them in guide. Strong field to collect charged decay products
- **Magnetic filter for improved systematics** – compensates absence of upstream detector
- **Pulsed neutron beam** to avoid regions of ill-defined spectrometer response (not needed for all observables)

Det



PERC



- Tunable selector field 3...6 T
- **Secondary spectrometers** optimized for observable
- Observables:
 - Electrons: A, b
 - Protons: a, C
 - Coincidences: no

- Target sensitivity: $\mathcal{O}(10^{-4})$
 - Individual systematic effects for PERC estimated $< 10^{-4}$
 - Depends on secondary spectrometer

• Installation in progress at FRM-II

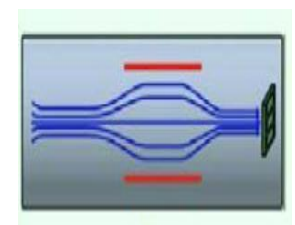
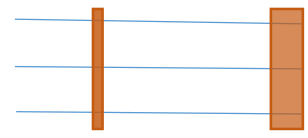
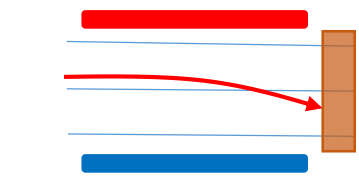
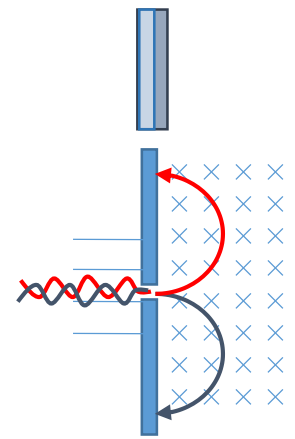
Electron detector

Magnetic spectrometer

Wien filter for protons

Electrostatic chopper & p detector

MAC-E filter



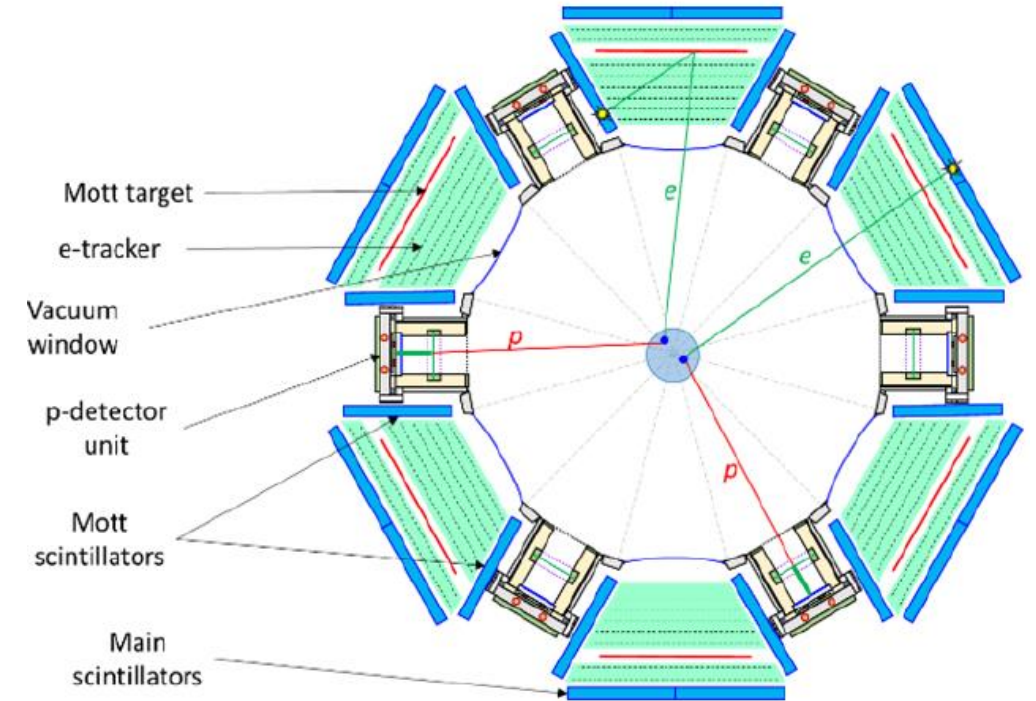
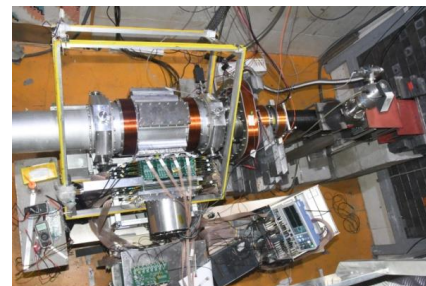
BRAND

Bodek et al, EPJ Web of Conf. 219 (2019) 04001

Abele et al, Phys. Rep. 1023 (2023) 1

Measure all correlations simultaneously

- Only existing project with **electron tracking** and **measurement of transversal electron polarisation**
- Access to yet **unmeasured correlations**
- **Independent systematics for measured correlations** (a, b, A, B, D)
- Based on **measurement of N, R** at PSI
- **Target statistical sensitivity:**
 - $5 \cdot 10^{-4}$ for coefficients involving electron polarisation
 - A few times 10^{-5} for a, A, B, D
- First tests of prototype components at PF1B, R&D ongoing



Reminder from start of lecture:

$$dW(\langle \sigma_n \rangle, \langle \sigma_e \rangle | E_e, \Omega_e, \Omega_\nu) \propto G_E(E_e) \cdot$$

$$\left\{ 1 + a \frac{p_e p_\nu}{E_e E_\nu} + \dots \right.$$

How to go further – ANNI @ ESS (proposal)

Pulsed beams are good for us!

§ Spatial localization of neutron pulse

- Separation of beam-related background
- Separation of ill-defined spectrometer response

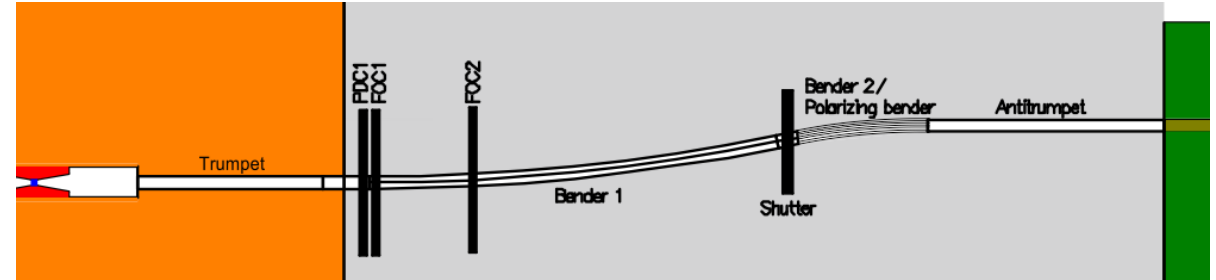
λ Separation by neutron wavelength

- Velocity dependence of signal and systematics
- Time-dependent neutron optics
- Loss-free monochromatization

τ Time localization of neutron pulse

- Improved signal/background
- Suppression of background and drifts with different time constant than signal

ANNI simulated gain factors (@ 5 MW)



Experiment	Facility	Gain	Event rate
NPDGamma	FnPB (SNS)	27	
PERC	MEPHISTO (FRM II)	15	
PERKEO III	PF1B (ILL)	17	
aSPECT	PF1B (ILL)		1.3 2.8

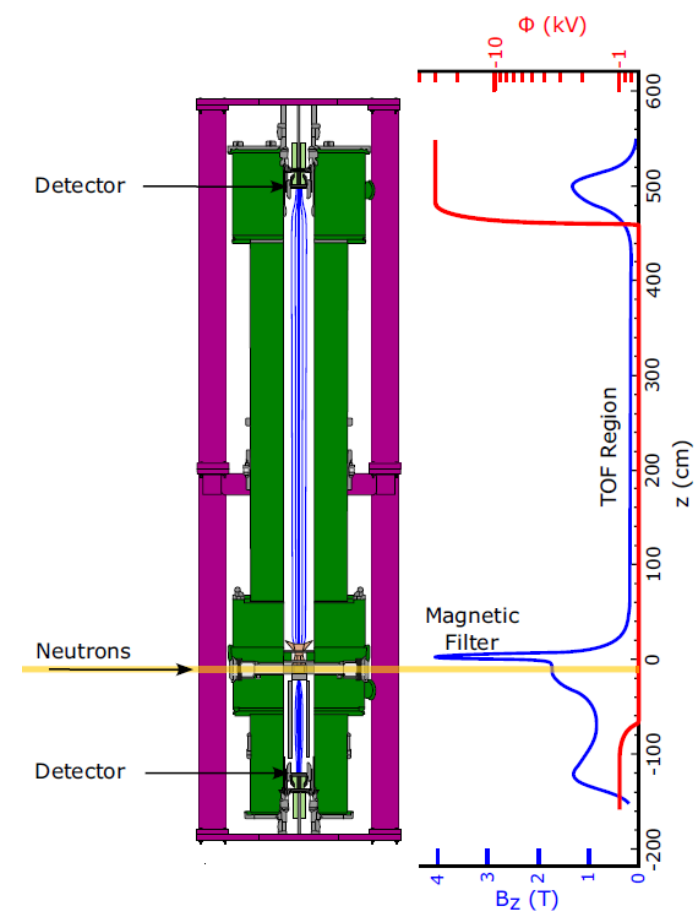
Status and outlook

Presently most precise experiment

- $\Delta a/a = 8 \cdot 10^{-3}$ [aSPECT 2020]
- $\Delta b = 0.02$ [PERKEO III 2020]
- $\Delta A/A = 1.7 \cdot 10^{-3}$ [PERKEO III 2019]
- $\Delta B/B = 5 \cdot 10^{-3}$ [Serebrov 98, PERKEO II 2008]
- $\Delta C/C = 1\%$ [PERKEO II 2007]
- $\Delta D = 2 \cdot 10^{-4}$ [emiT 2012]
- $\Delta R = 0.013$ [Kozela 2012]

Ongoing projects

- **Nab @ SNS: a, b**
 - First data taken
 - Goals: $\Delta a/a \approx 0.1\%$, $\Delta b \approx 0.003$
 - Proposal for pNab
- **PERC @ FRM-II: A, b, a, C**
 - Installation in progress
 - Goals: a few times 10^{-4}
- **BRAND @ ILL / ESS: $a, A, B, D, H, L, N, R, S, U, V$**
 - R&D ongoing
 - Goals: a, A, B, D : not limited by stat (few times 10^{-5})
 H, L, \dots (with transversal electron polarization): $5 \cdot 10^{-4}$



Hayen et al, Phys. Rev. C 107 (2023) 065503
Baessler et al, J. Phys. G 41 (2014) 114003